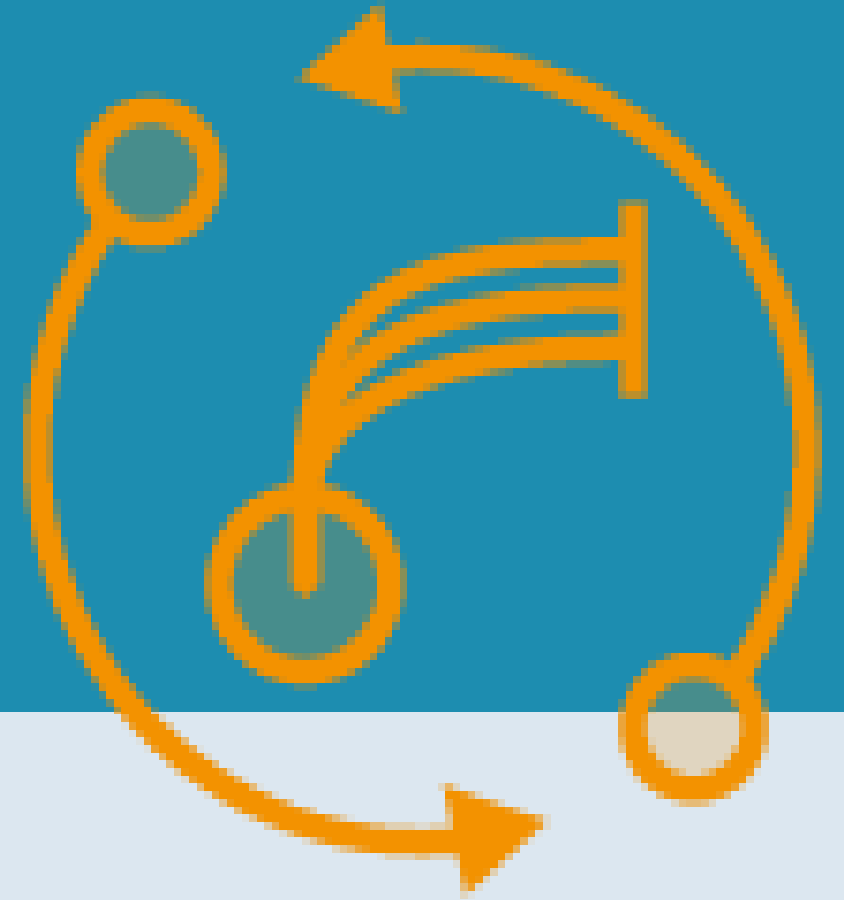


# Basics of Radioactive Ion Beam production

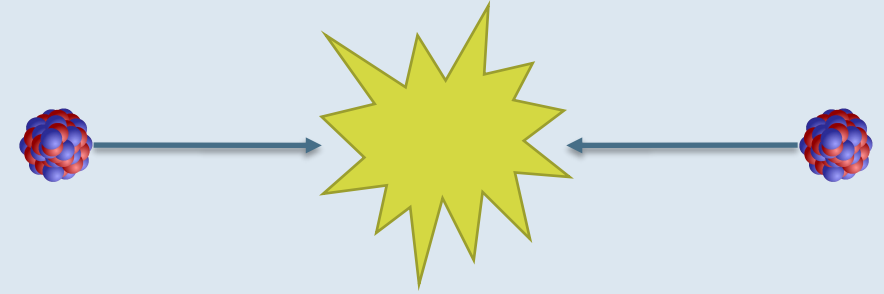
Chair Roger Van Geen  
Lecture 1 – 25 October 2021



# Outline of this lecture

- Nuclear reactions for the production of radioisotopes
- Luminosity & cross sections
- Examples across the nuclear landscape
  - Industrial production
  - Towards  $^{100}\text{Sn}$
  - Superheavy elements

# Nuclear reactions



# 2 big families

## Adding stuff

- Starting with any nucleus, you can add particles to it to make a new, heavier nucleus.
- Possible approaches are neutron capture, proton capture, etc. and particle transfers.
- Things do not always go as planned and those particles may either not stick or the produced nucleus may decide to shed away particles: fusion-evaporation.

## Breaking stuff

- Starting with something rather big, it is possible to break it into smaller pieces.
- Depending on the process that triggers this breakdown, we speak about fragmentation, spallation, or fission.
- Each process leads to a different distribution of the end products.
- The different channels may be in competition with each other.

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Text **THOMASELIASC687** to **+32 460 20 00 56** once to join

# What is best to induce nuclear reaction

Photon

Electron

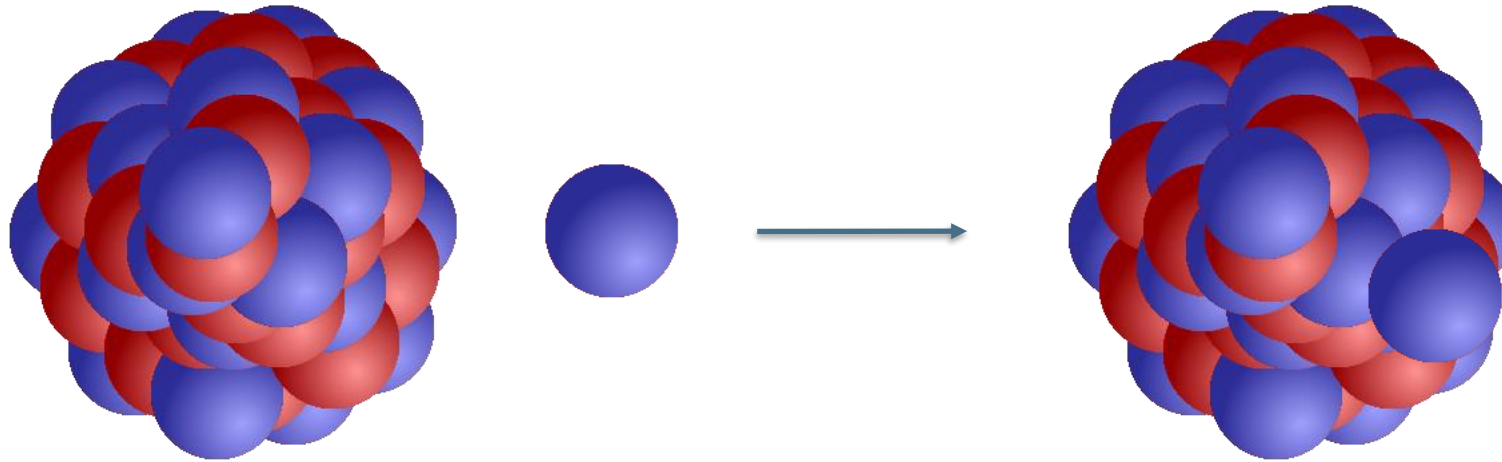
Proton

Neutron

Heavy ion

Start the presentation to see live content. For screen share software, share the entire screen. Get help at [pollev.com/app](https://pollev.com/app)

# Neutron capture reactions



${}^A\text{X}_N$  + neutron

${}^{A+1}\text{X}_{N+1}$

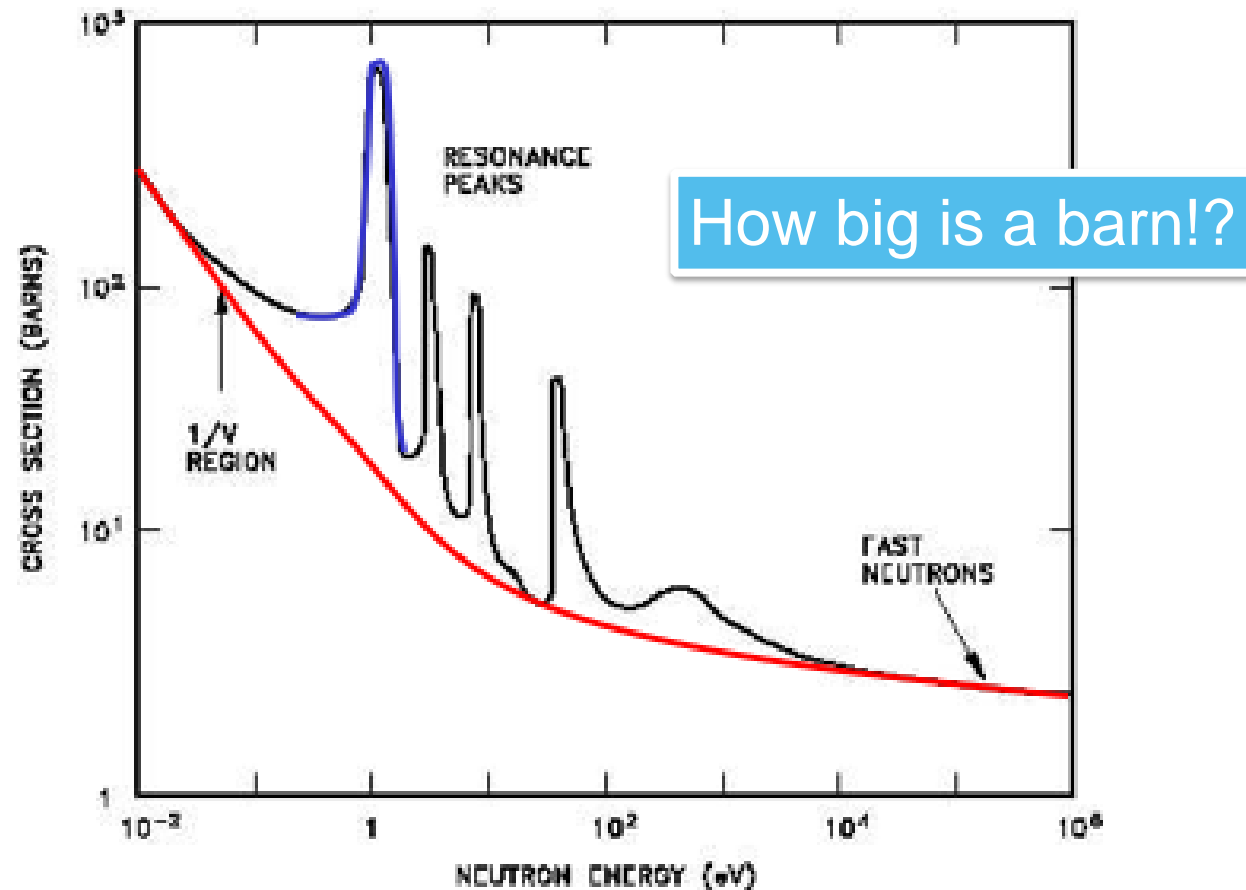
## neutron capture:

- Same element, new isotope
  - Neutron has no charge and must not overcome the Coulomb barrier
- Reaction can occur from low energy

What is the most efficient E?

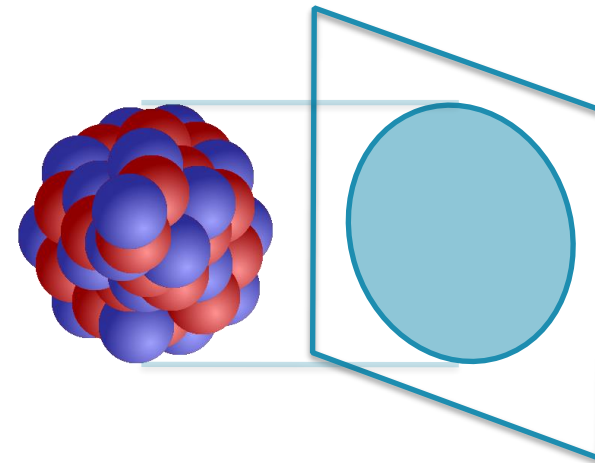
# Neutron capture cross sections

- 2 types of reactions: non-resonant and resonant
- Non-resonant reactions scale as  $1/v$ , favouring slow neutrons over fast neutrons  
→ 100b → 1b
- Resonant reactions have a Lorentz profile centred around a specific energy, and having an associated width and intensity
- ~100b



# Reaction cross sections

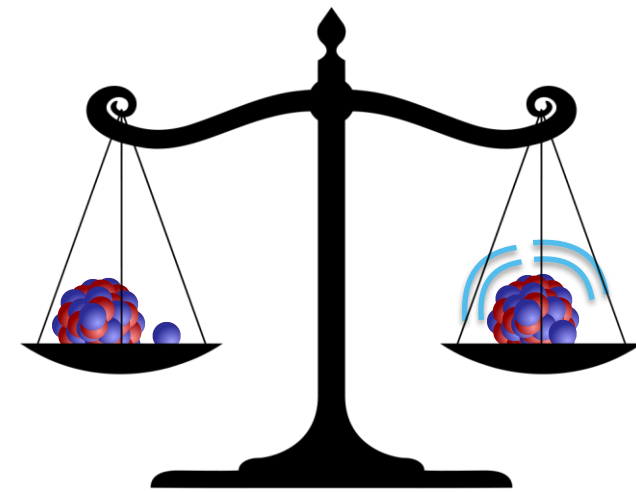
- 1 barn =  $10^{-24}\text{cm}^2$
- 1 barn =  $10^{-28}\text{m}^2$  (SI)
- 1 barn =  $100\text{fm}^2$
- Defines the area that a particle may hit
- 1 barn ~ 2D projection of a nucleus of uranium, corresponding to a radius of 5.64fm
- It is now the measure of the probability of a reaction to occur (nuclear & particle physics)



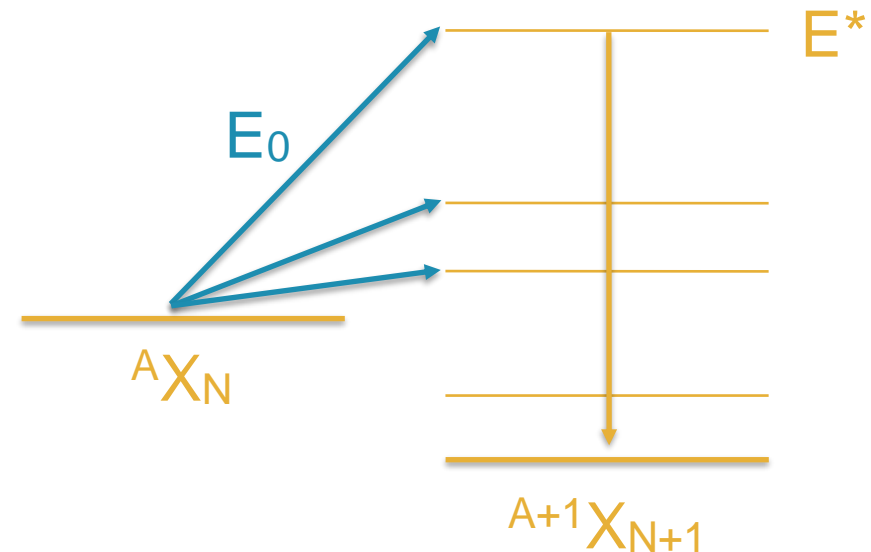


# Resonant neutron capture

- The combined energy of the neutron and the nucleus corresponds to an excited state in the new nucleus
- The excited state decays away by any mode that is possible, according to its own properties. This may include  $\gamma$  decay to lower excited states down to the ground state.



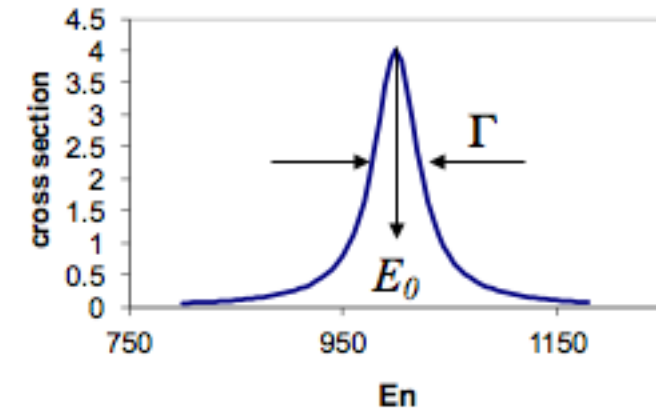
$$E_0 + BE[^AX_N] = E^* + BE[^{A+1}X_{N+1}]$$



# Resonant neutron capture cross section

- It follows the Breit-Wigner formula
- $\Gamma$  is the width of the excited level
- The width scales with the half-life:  $\Gamma = \frac{\ln(2)}{T_{1/2}}$
- $(E_n - E_0)$  is the neutron energy detuning
- The formula needs to account for all the possible decay channels from  $E^*$  besides  $\gamma$ -ray emission: particle emission, fission, ...

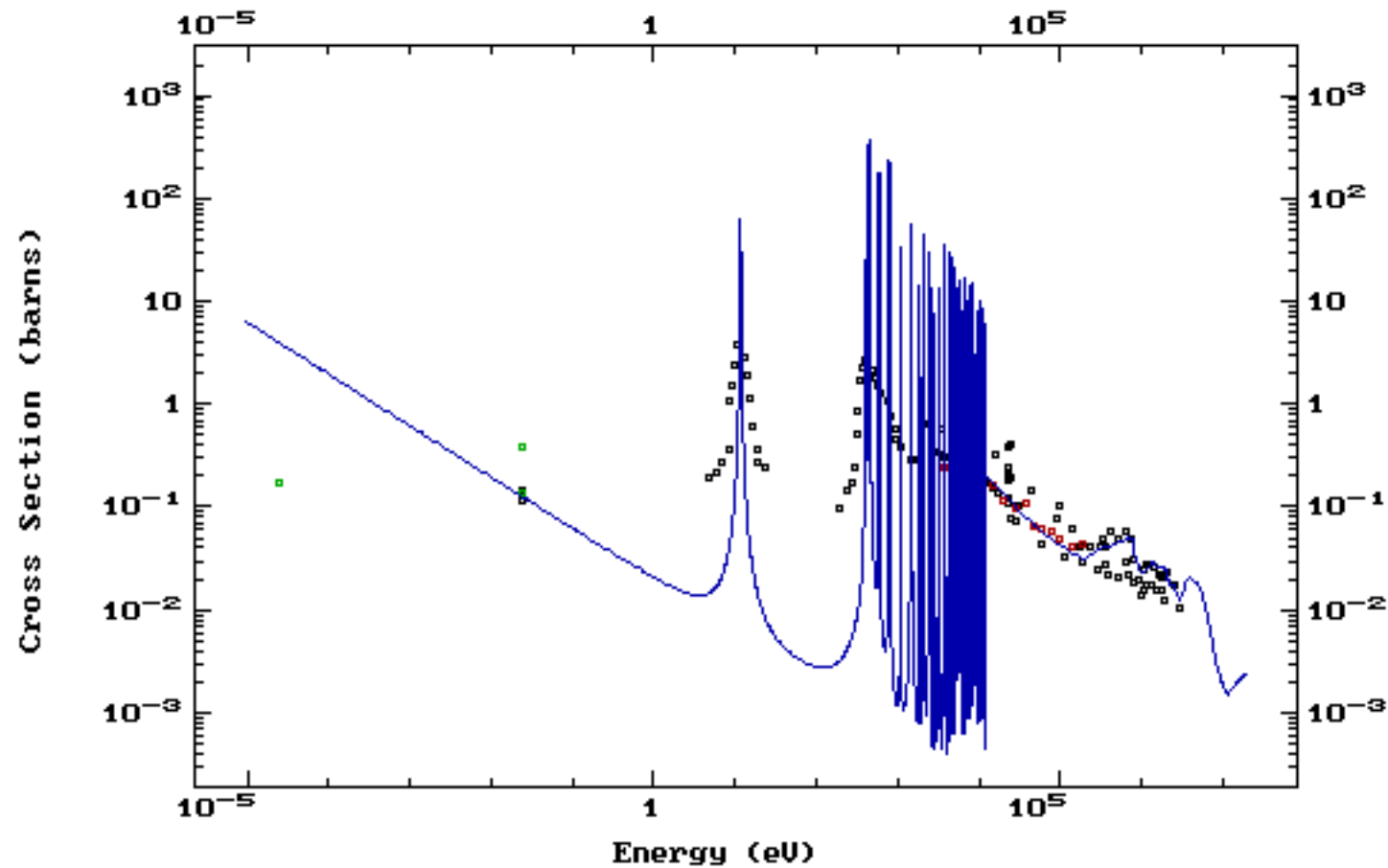
$$\sigma \sim \frac{\Gamma^2}{(E_n - E_0)^2 + \Gamma^2 / 4}$$



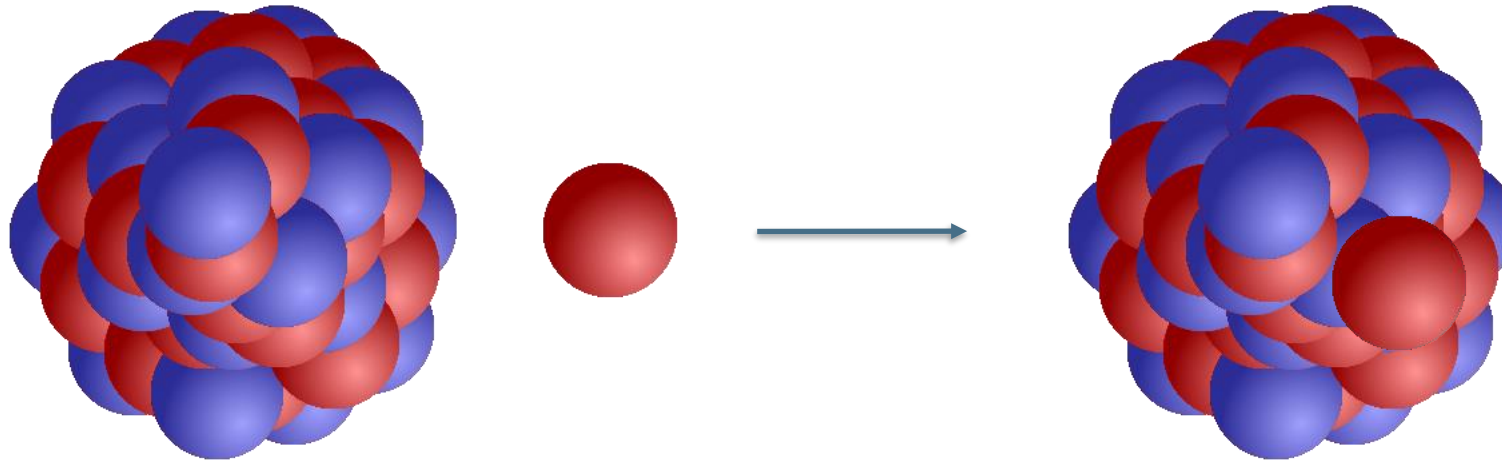
$$\sigma \sim \frac{\Gamma \Gamma_\gamma}{(E - E_0)^2 + \Gamma^2 / 4}$$

# Neutron capture: $^{98}\text{Mo} (n,\gamma) ^{99}\text{Mo}$

Mo-98(n,γ)Mo-99  
1.0000+00\* JEF-2.2



# Proton capture reactions



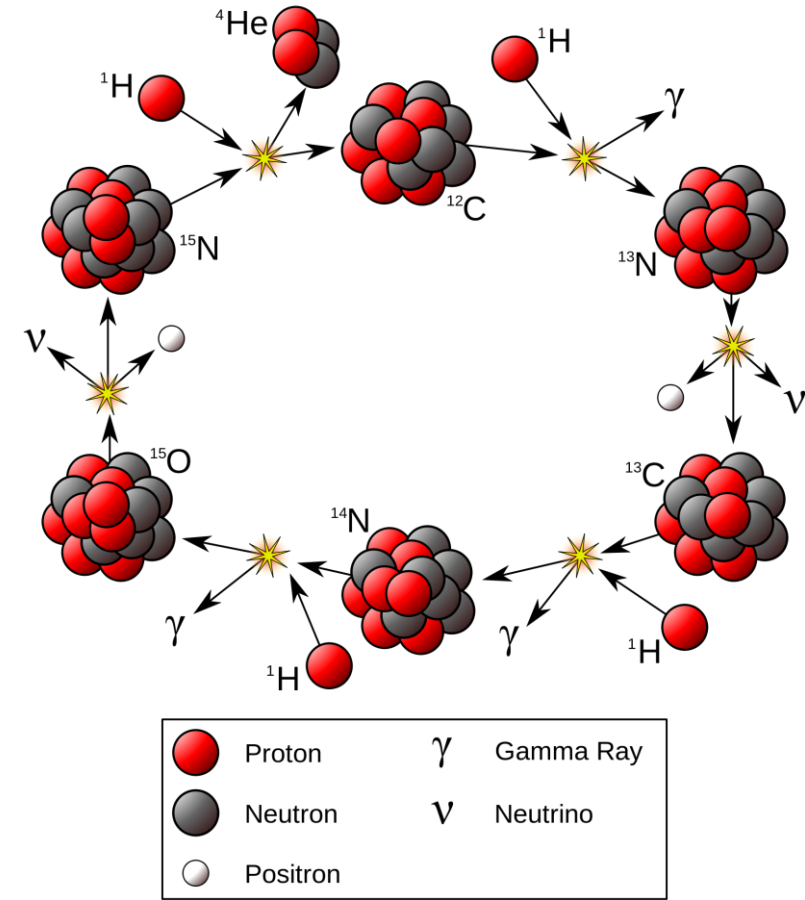
## proton capture:

- Different element, different isotope
- Proton must overcome the Coulomb barrier  
→ Reactions require a powerful driver

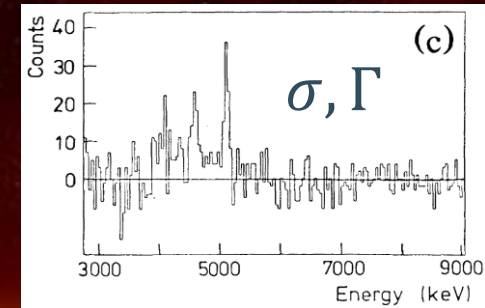
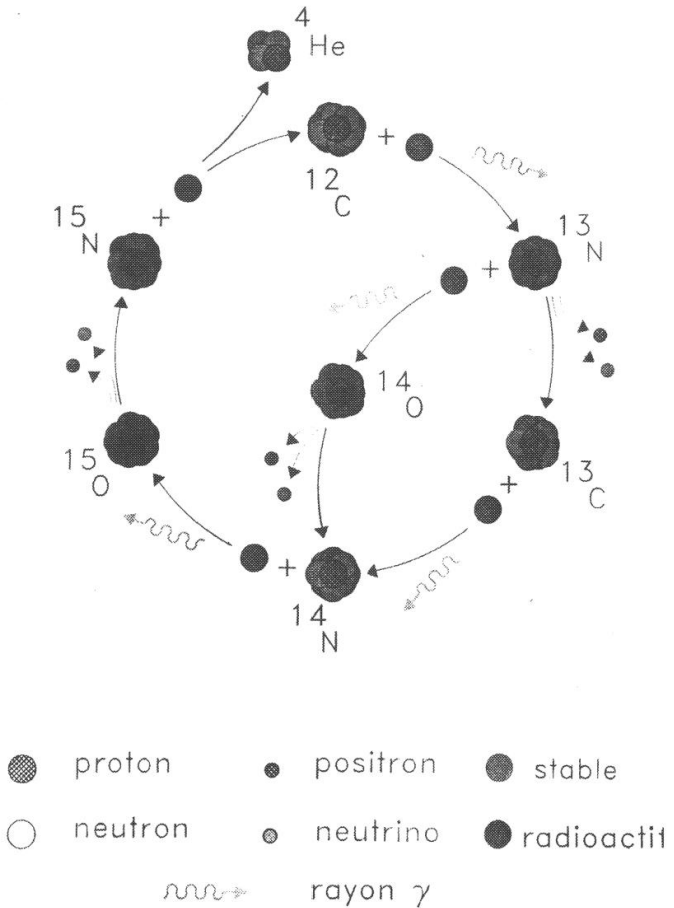
What happens if the driver is too powerful?

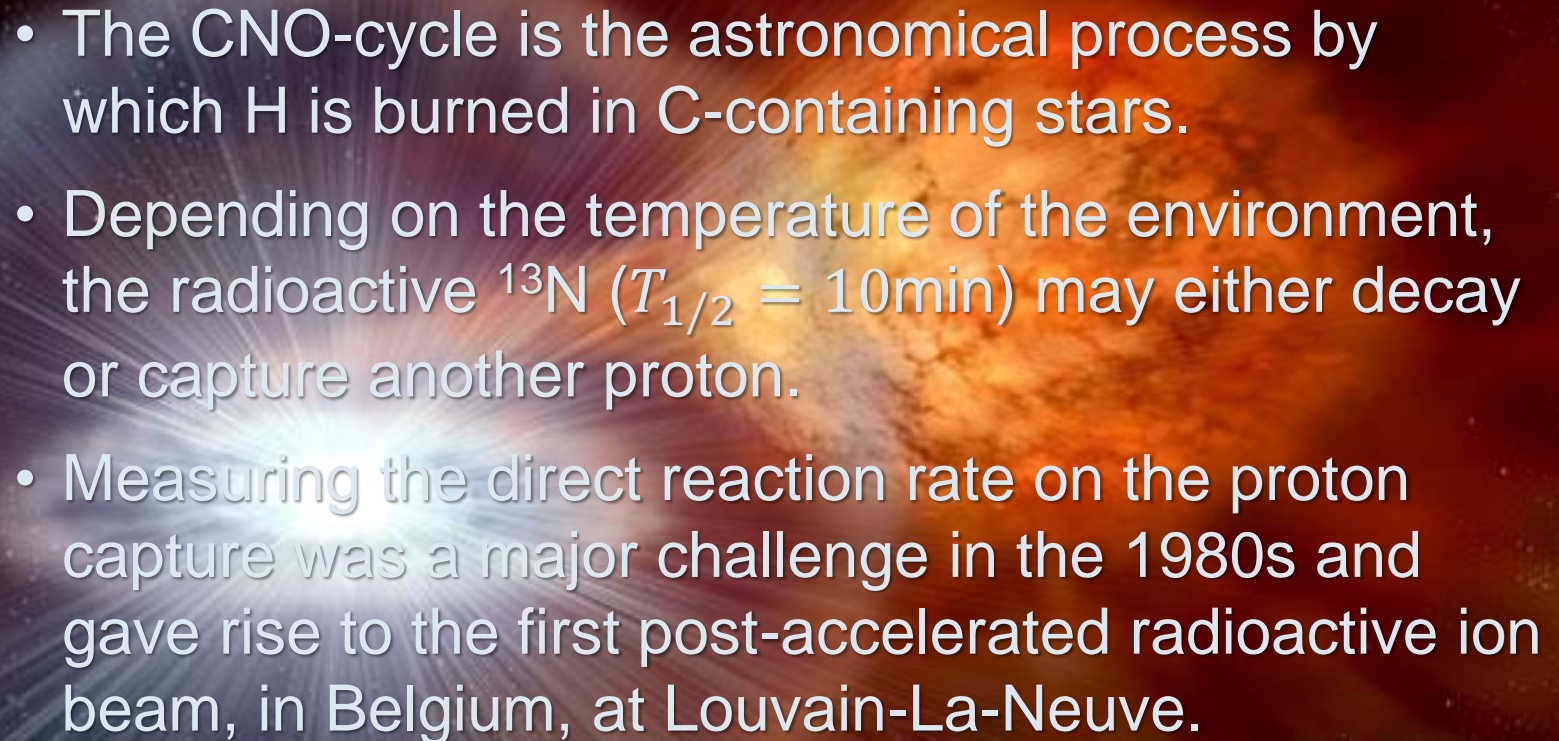
# Resonant proton radiative capture

- Similar to resonant neutron capture, including the Coulomb barrier in the energy balance
- Only valid over a small number of states of well-defined energies
- Mostly interesting for astrophysical purpose to understand star burning processes such as the CNO cycle



# $^{13}\text{N}(p,\gamma)^{14}\text{O}$ : the hot-CNO cycle

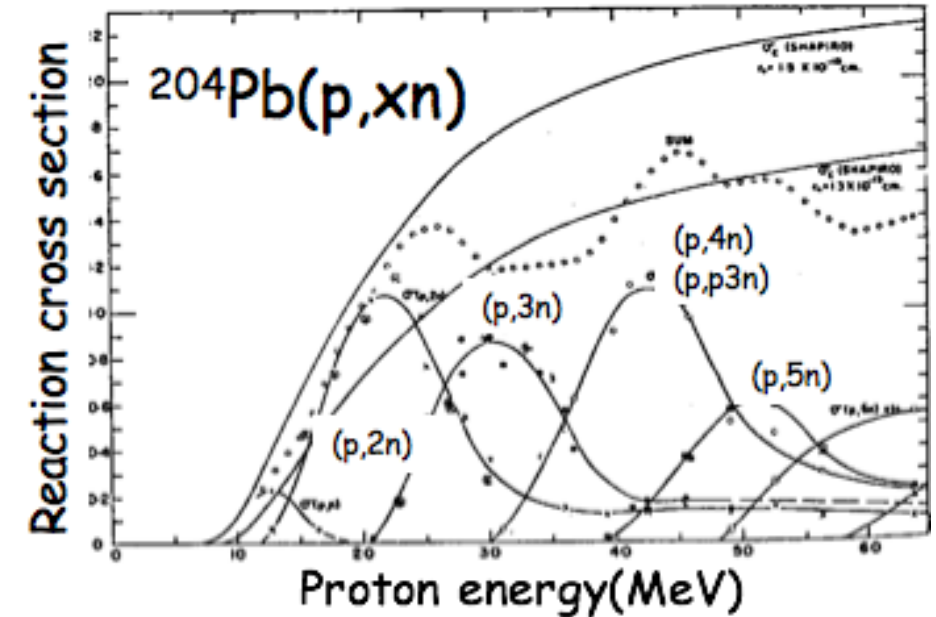
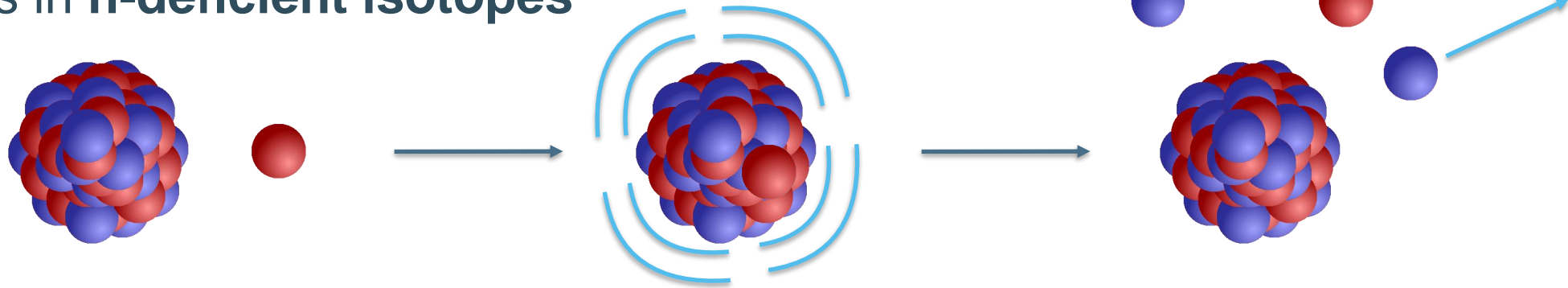


- 
- The CNO-cycle is the astronomical process by which H is burned in C-containing stars.
  - Depending on the temperature of the environment, the radioactive  $^{13}\text{N}$  ( $T_{1/2} = 10\text{min}$ ) may either decay or capture another proton.
  - Measuring the direct reaction rate on the proton capture was a major challenge in the 1980s and gave rise to the first post-accelerated radioactive ion beam, in Belgium, at Louvain-La-Neuve.



# Proton fusion-evaporation

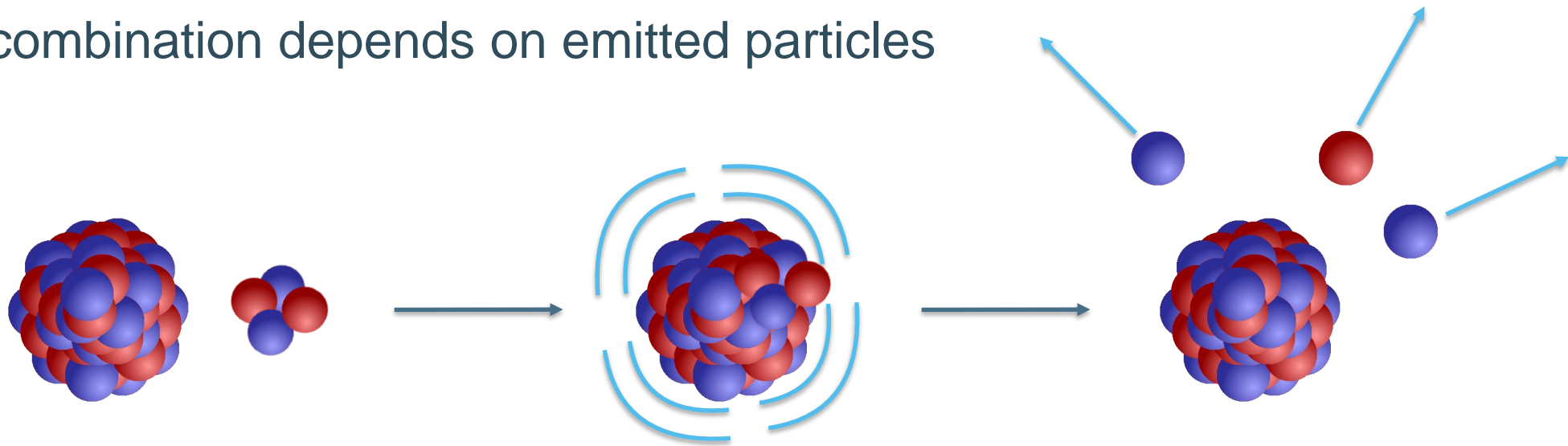
- The proton brings so much energy that the compound nucleus is excited beyond the particle emission threshold
- The system is particle-unbound and the particle emission wins over the radiative capture
- Results in **n-deficient isotopes**



# Heavy ion fusion-evaporation



- Same concept as the proton fusion-evaporation reaction, but using larger projectiles, such as  $\alpha$  particles or heavy ion beams
- Beam with  $Z_b, N_b$ ; target with  $Z_t, N_t$ 
  - Compound nucleus with  $Z_c = Z_b + Z_t$ ;  $N_c = N_b + N_t$
  - Final combination depends on emitted particles





# Fusion-evaporation formalism

## Energy considerations

$$E_{\text{beam}} = E_{\text{Coulomb}}(Z_b, Z_t) + X(\zeta n, \xi p)$$

- You need to break through the Coulomb barrier, which goes typically to ~3-4 MeV/u for heavy ion beams
- The number of particles  $\zeta$  &  $\xi$  evaporated depends upon how much energy is brought in, with ~10 MeV per nucleon evaporated

## Cross section

- Each target/beam/energy combinations will yield to different outcomes
- Compare on the right the production of  $^{62}\text{Cu}$ 
  - ♦  $^{60}\text{Ni}(\alpha, pn)$  :  $E_c \sim 3 \times 4 = 12$  MeV;  $X(1,1) \sim 20$  MeV
  - ♦  $^{63}\text{Cu}(p, pn)$  :  $E_c \sim 3 \times 1 = 3$  MeV;  $X(1,1) \sim 20$  MeV
- Many things may be produced with a single combination

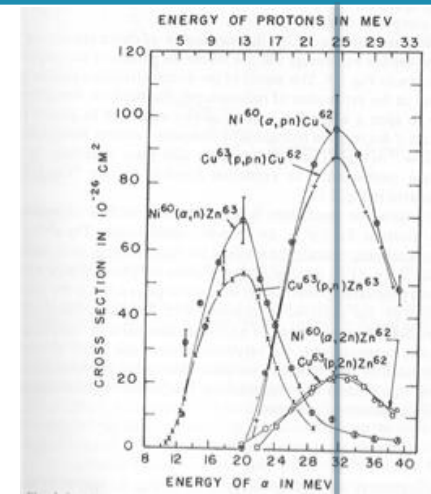
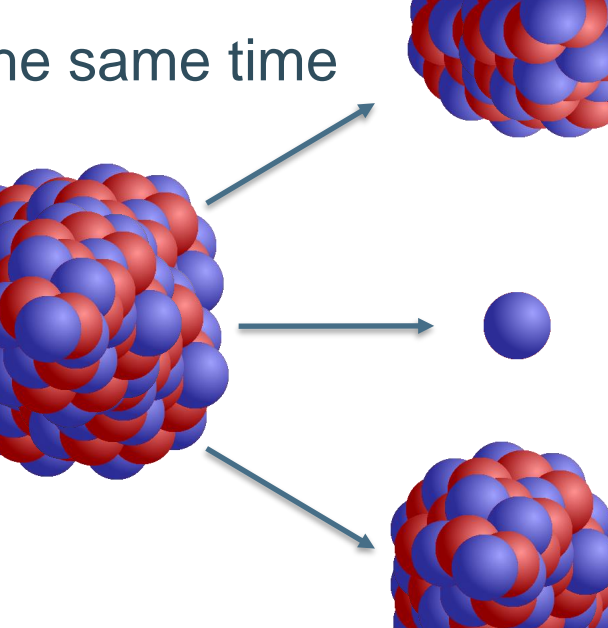
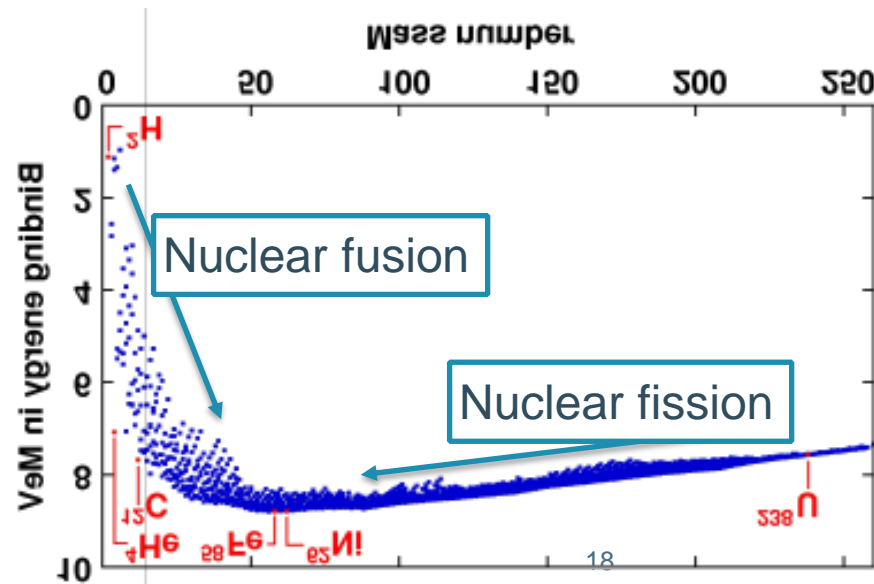


Diagram illustrating the alpha-decay chain of  $^{238}\text{U}$  to  $^{106}\text{Mo}$  via  $^{132}\text{Sn}$ . The chain is shown as a green loop connecting the three isotopes.

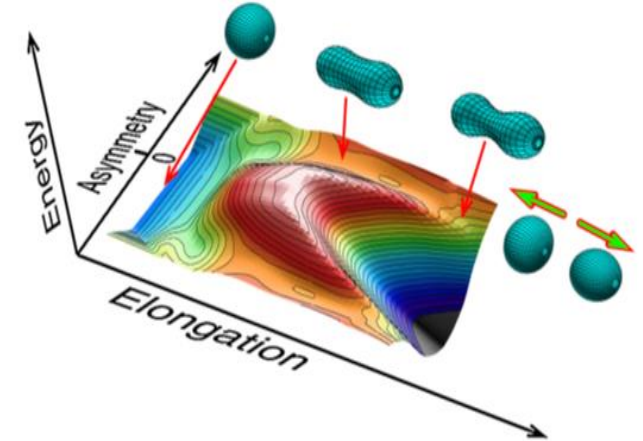
- at the same time
- 
- The diagram illustrates a nuclear fission reaction. On the left, a large, roughly spherical nucleus is composed of many smaller spheres, colored red and blue. Three arrows originate from this nucleus and point towards the right. The top arrow points to a medium-sized nucleus, the middle arrow points to a single small blue sphere (a neutron), and the bottom arrow points to another medium-sized nucleus. These two medium-sized nuclei are also composed of red and blue spheres, similar to the original nucleus but smaller. The text 'at the same time' is positioned above the top arrow.



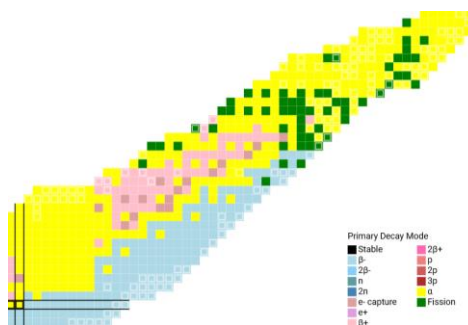
# Nuclear fission

## Fission barrier

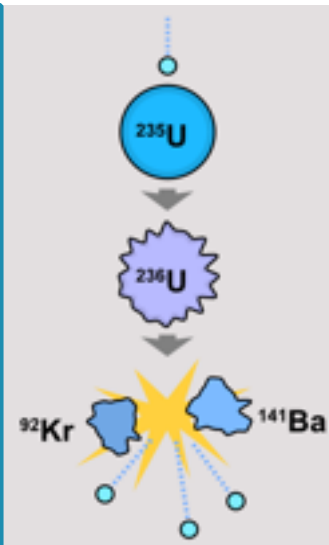
- Nuclei are bound to a local energetic minimum.
- To undergo fission, they have to overcome an energy wall beyond which more energy can be gained.
- Depending on the height of the barrier, fission can happen spontaneously, be induced by thermal neutrons, or require high energy bombardment.



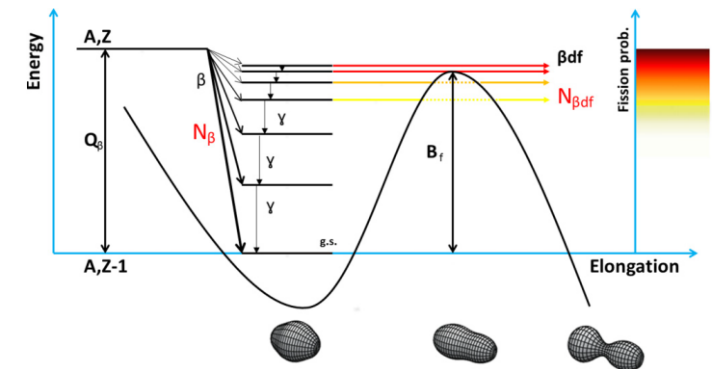
Spontaneous fission is found in the very & super heavy elements.



Particle-induced is most commonly used. Research with  $\gamma$ -induced fission has been done as well.



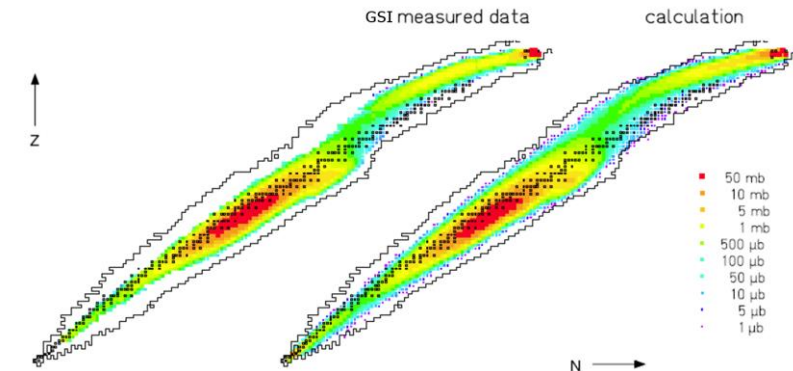
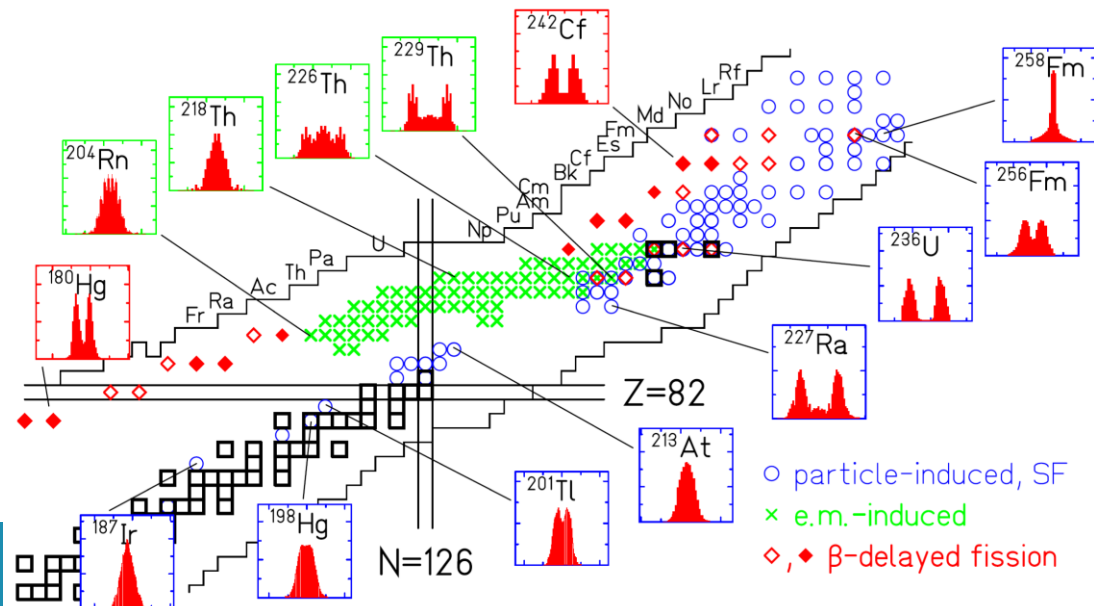
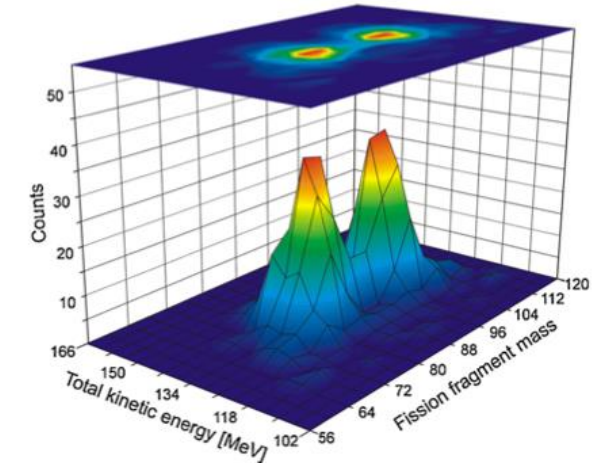
$\beta$ -delayed fission can compete with  $\gamma$  decay



# Fission fragments distribution

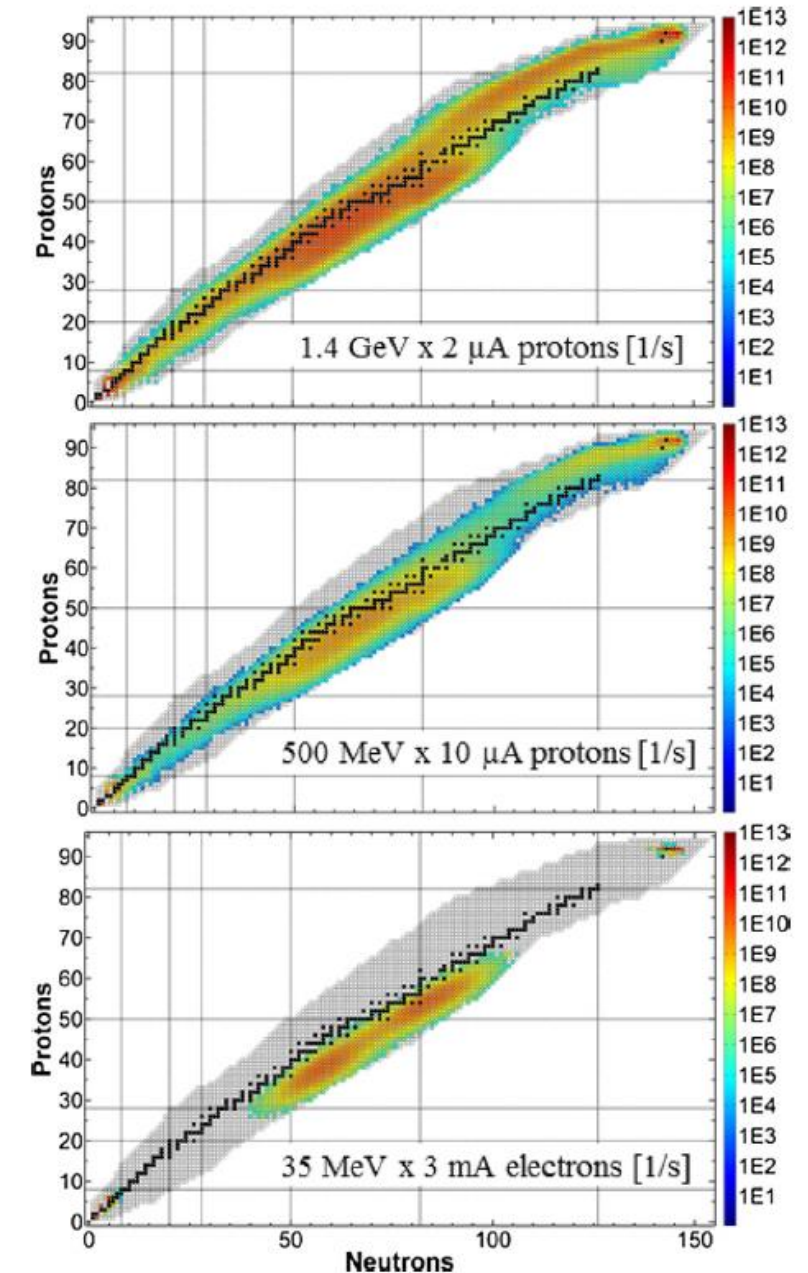
## Fission fragments

- They keep the same  $N/Z$  balance as the parent nucleus  
→ Produces mostly **n-rich isotopes**
- The fission may be symmetric or asymmetric depending upon energy considerations (parent's excitation energy, nuclear structure of the fragments)

1GeV protons on  $^{238}\text{U}$  in inverse kinematics

# Fission of $^{238}\text{U}$

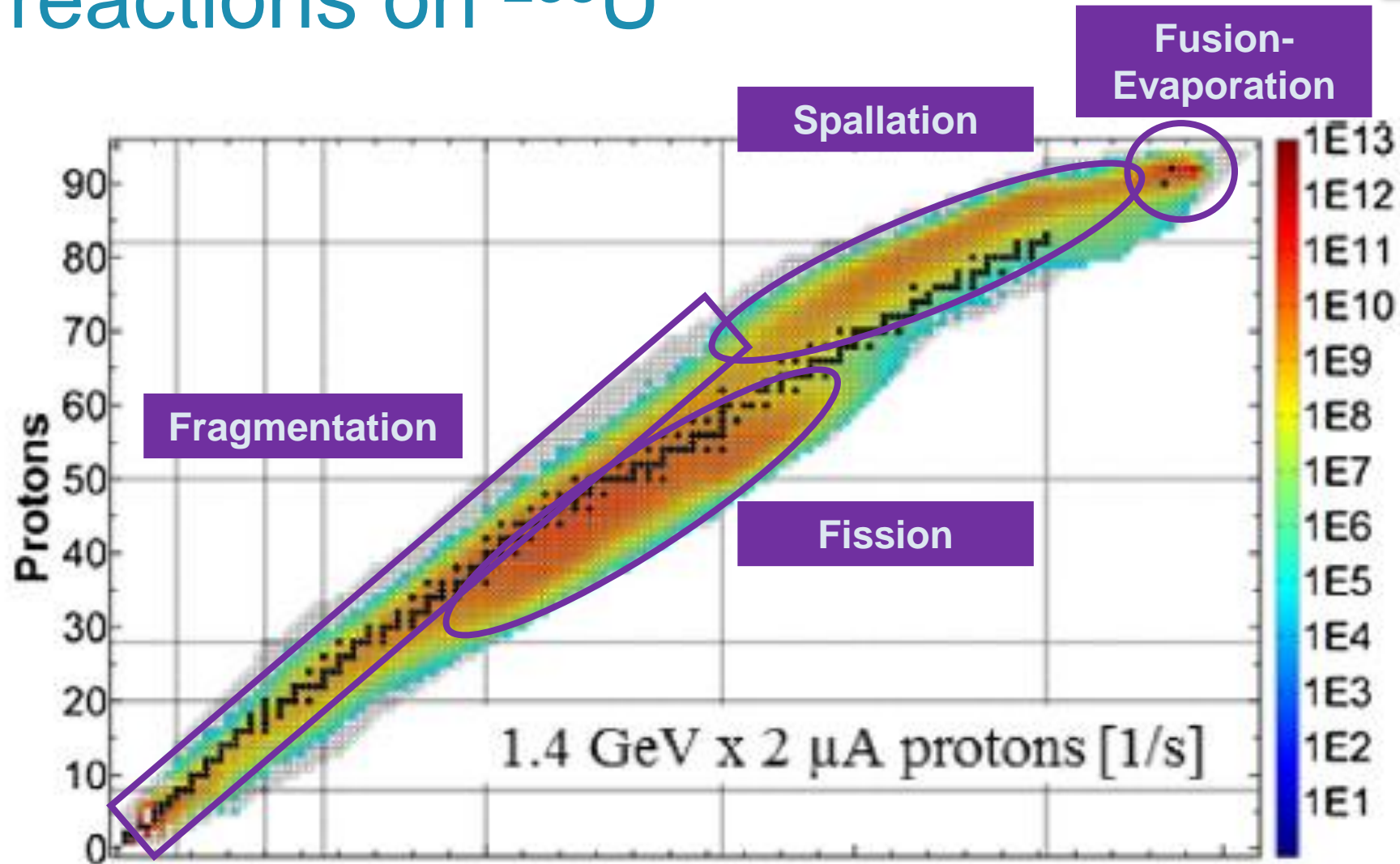
- $^{238}\text{U}$  is the most neutron-rich isotope that is easily available and with which to make a target. It is therefore the target of choice for the production of exotic radioisotopes.
- $^{252}\text{Cf}$  is a very interesting alternative, however it cannot be used with as high quantities as  $^{238}\text{U}$ .
- Particle energy and type have a big impact on the fragment distribution.





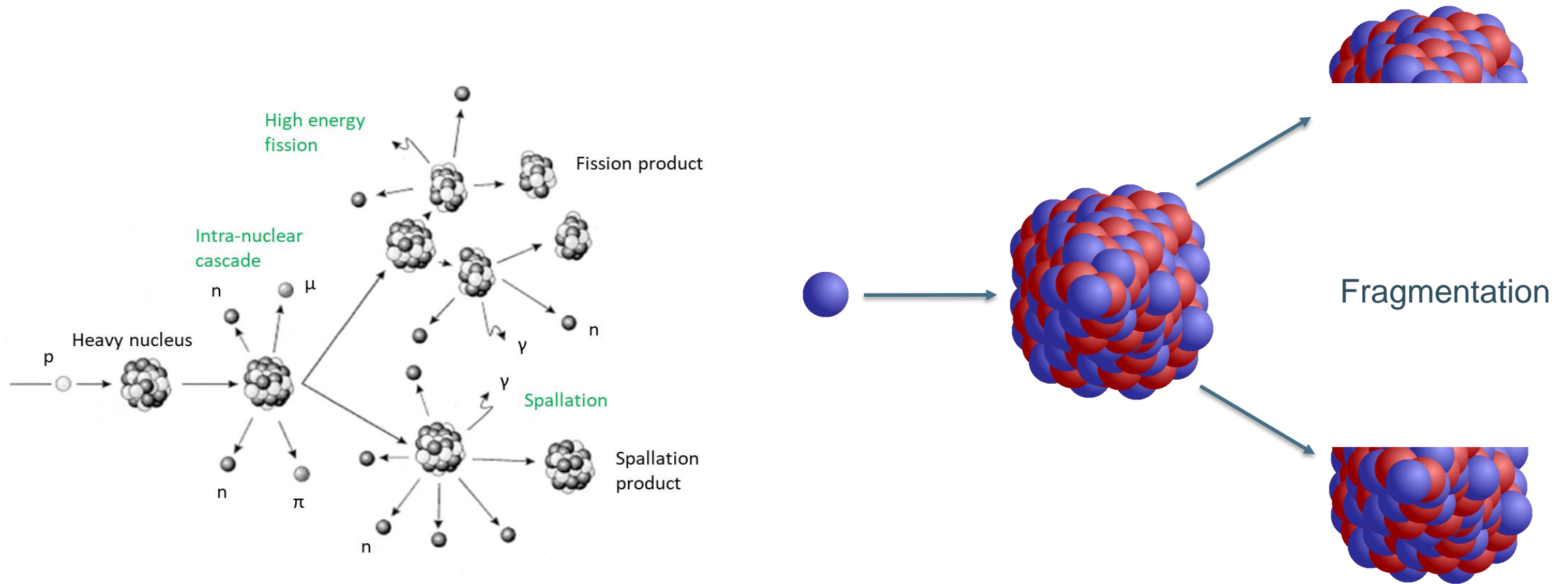
# Other reactions on $^{238}\text{U}$

$^{238}\text{U}$  (p,x)



... and many more  
secondary reactions

# Multiple reaction channels



# Luminosity & cross sections

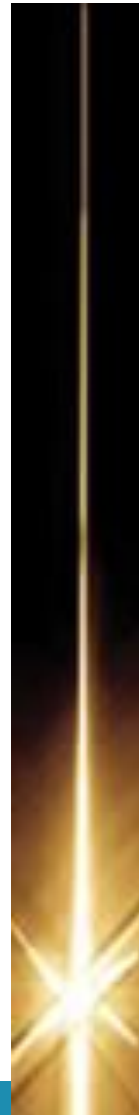




# Luminosity in beam-induced reactions

- The luminosity is the unbiased measure of the reaction ingredients
  - ▶ number of incoming beam particles  $N_b$
  - ▶ density of the target  $d_t$
  - ▶ thickness of the target  $a_t$
  - ▶  $d_t a_t$  is the number of target atoms per unit area

$$L = N_b \cdot d_t a_t$$



- The luminosity can also be determined in terms of more practical parameters
  - ▶ beam flux  $\varphi = N_b / S$ , where  $S$  is the beam spot size
  - ▶  $U = S d_t a_t$  is the number of target atoms within the beam spot

$$L = \varphi \cdot U$$

# Beam-induced nuclear reactions

## Production:

- Nuclear reaction scales with the cross section  $\sigma$
- Nuclear reaction scales with the luminosity  $L$

$$\begin{aligned}\frac{dn}{dt} &= +L\sigma \\ &= +N_b \cdot d_t a_t \cdot \sigma\end{aligned}$$

## Destruction:

- Radioactive decay is a net loss in the population
- Radioactive decay goes inverted to the decay half-life

$$\begin{aligned}\lambda &= \frac{\ln 2}{T_{1/2}} \\ \frac{dn}{dt} &= -\lambda n\end{aligned}$$

$$\frac{dn}{dt} = +N_b \cdot d_t a_t \cdot \sigma - \lambda n$$

# Beam-induced nuclear reactions

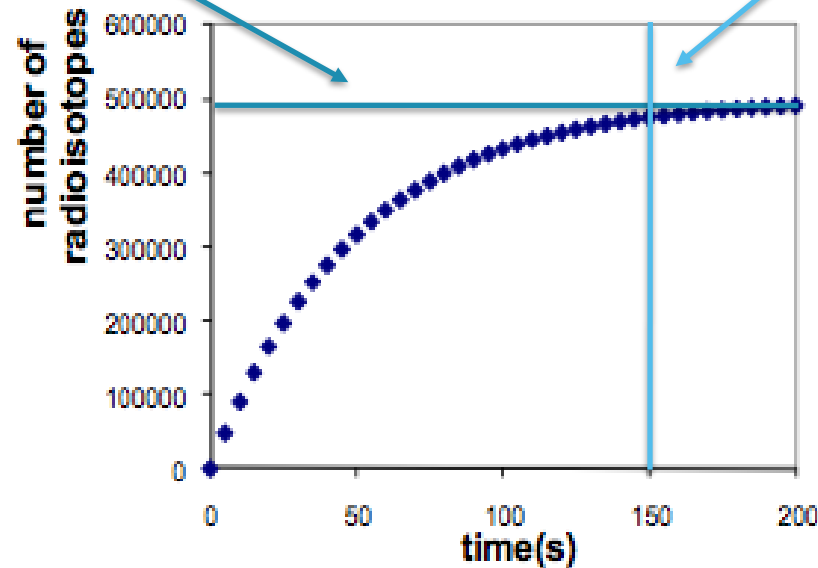
$$n(t) = \frac{N_b \cdot d_t a_t \cdot \sigma}{\lambda} (1 - e^{-\lambda t})$$

Saturation level depends on

- Beam intensity  $N_b$
- Target atoms  $d_t a_t$
- Cross section  $\sigma$
- Half-life

Saturation time depends on

- Half-life



Saturation is reached after 3 lifetimes

$$T_S = 3\tau = \frac{3}{\lambda} = 3 \frac{T_{1/2}}{\ln 2}$$

# Activity

What assumptions are made for this solution?

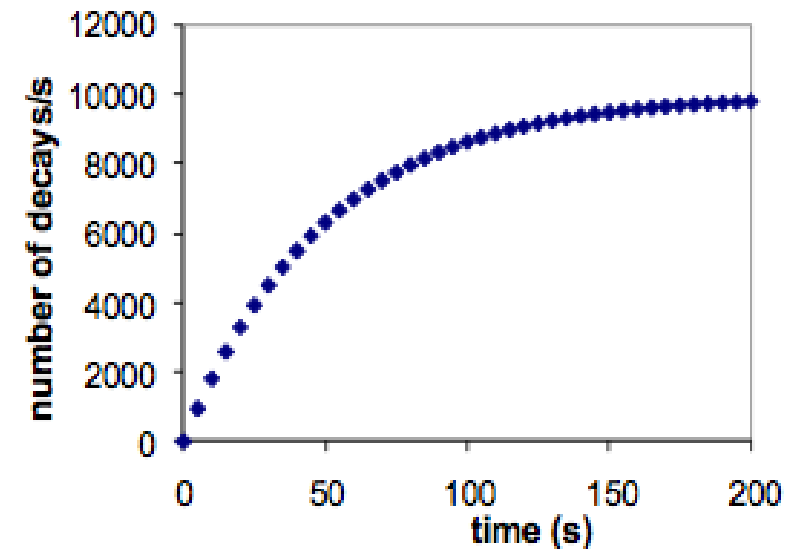
## Nuclear activity:

- Number of radioactive decays per unit time in Bq [decays/s]

$$A = \lambda n(t)$$

$$A = N_b \cdot d_t a_t \cdot \sigma (1 - e^{-\lambda t})$$

- The activity saturates also after 3 lifetimes
- The maximum activity is independent of the half-life, and only depends on the cross section and luminosity
- The time it takes to reach this activity still depends on the half-life



# Neutron-capture reactions

High neutron flux  $\varphi$ :

- If the neutron flux  $\varphi$  is high enough, the target material  $U$  is turned into something new,  $n$ , and disappears:

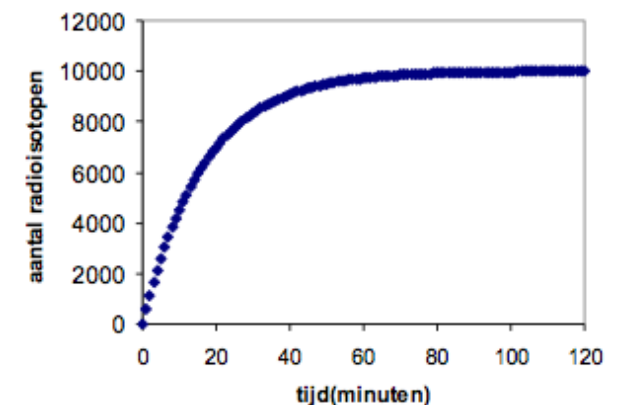
$$\frac{dU}{dt} = -\varphi \cdot \sigma \cdot U(t) \qquad U(t) = U_0 e^{-\varphi \sigma t}$$

Long half-life limit:

- Assuming that the half-life of the daughter is so long that we may neglect the decay:

$$n(t) = U_0 (1 - e^{-\varphi \sigma t})$$

- The saturation level depends only on the number of target atoms  
→ complete transmutation!
- Saturation time depends on flux and cross section
- Activity is proportional to  $\lambda$ , which depends on  $T_{1/2}$



# Neutron-capture reactions

Considering radioactive decay:

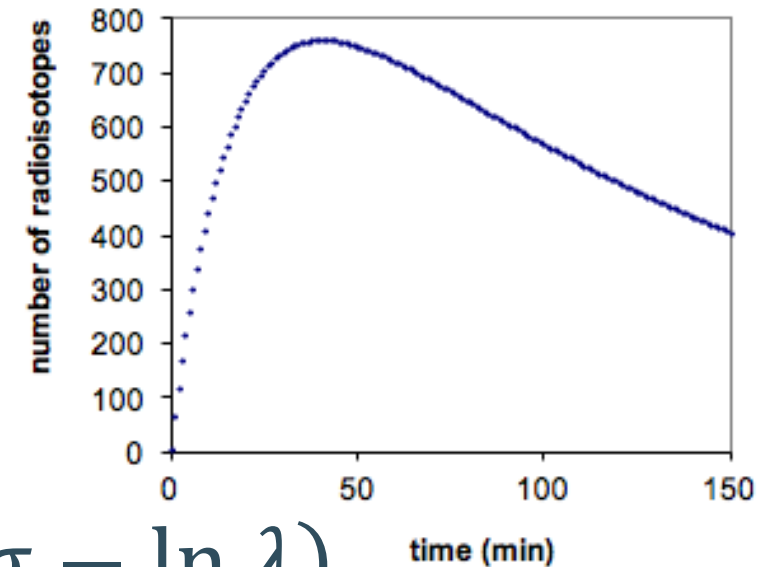
- The reaction differential equation becomes:

$$\frac{dn}{dt} = \varphi \cdot \sigma \cdot U(t) - \lambda n(t) = \varphi \cdot \sigma \cdot e^{-\varphi \sigma t} - \lambda n(t)$$

$$n(t) = \frac{\varphi \sigma U_0}{\varphi \sigma - \lambda} (e^{-\lambda t} - e^{-\varphi \sigma t})$$

- The production does not saturate but instead reaches a maximum

$$\frac{dn}{dt}(t_{max}) = 0 \Rightarrow t_{max} = \frac{1}{\varphi \sigma - \lambda} (\ln \varphi \sigma - \ln \lambda)$$



# Neutron capture & activity

## Production

$$n(t) = \frac{\varphi\sigma U_0}{\varphi\sigma - \lambda} (e^{-\lambda t} - e^{-\varphi\sigma t})$$

- builds up until  $t_{max}$
- max value scales up with  $T_{1/2}$
- for very long-lived isotopes, there can be as much as  $U_0$

## Activity

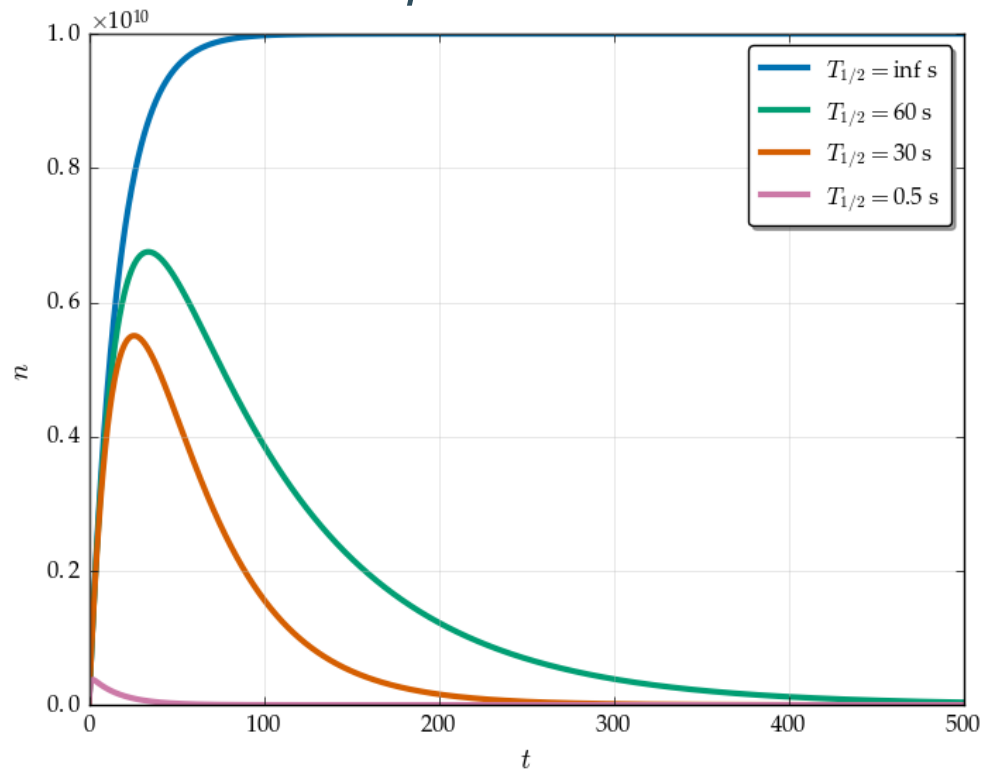
$$A(t) = \lambda \frac{\varphi\sigma U_0}{\varphi\sigma - \lambda} (e^{-\lambda t} - e^{-\varphi\sigma t})$$

- max value at the same  $t_{max}$
- max values scales down with  $T_{1/2}$

# Neutron capture & activity

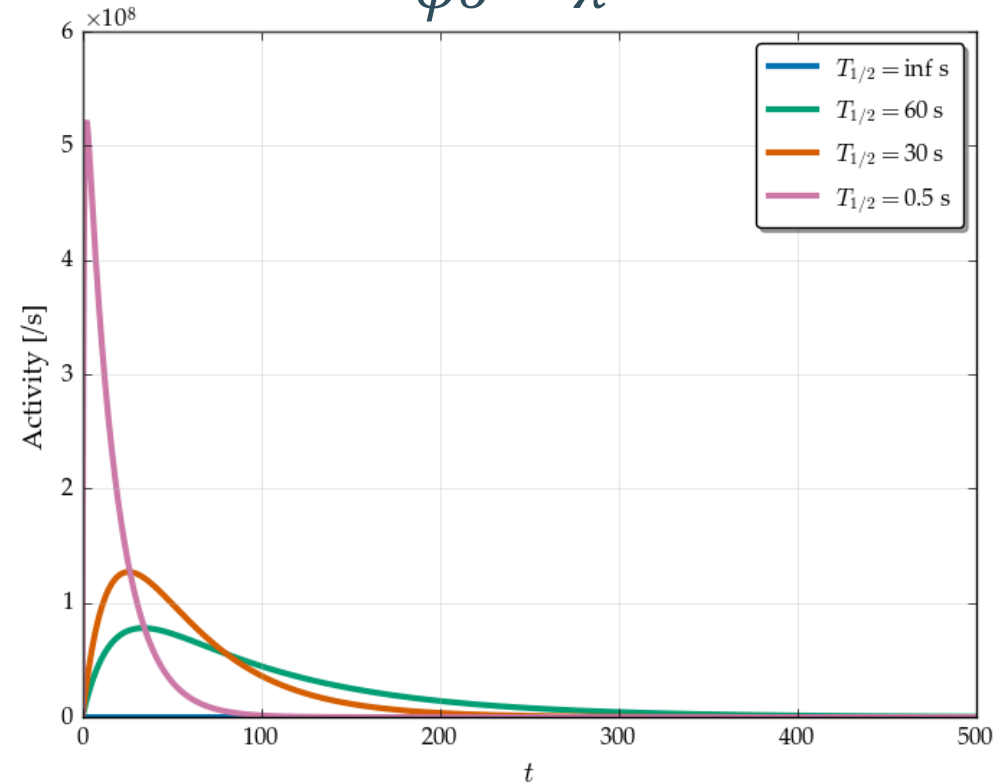
## Production

$$n(t) = \frac{\varphi\sigma U_0}{\varphi\sigma - \lambda} (e^{-\lambda t} - e^{-\varphi\sigma t})$$



## Activity

$$A(t) = \lambda \frac{\varphi\sigma U_0}{\varphi\sigma - \lambda} (e^{-\lambda t} - e^{-\varphi\sigma t})$$

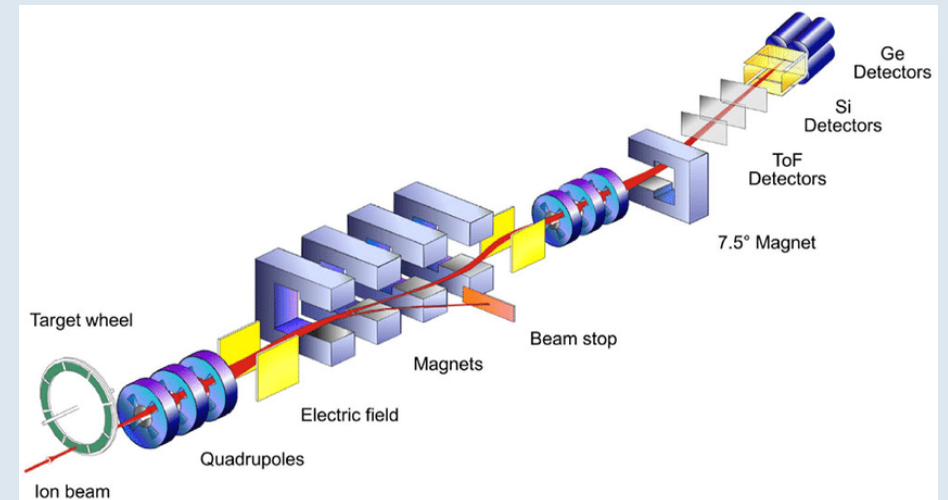




# BREAK

# Specific examples

- Industrial production
- Towards  $^{100}\text{Sn}$
- Reaching out to the superheavy elements



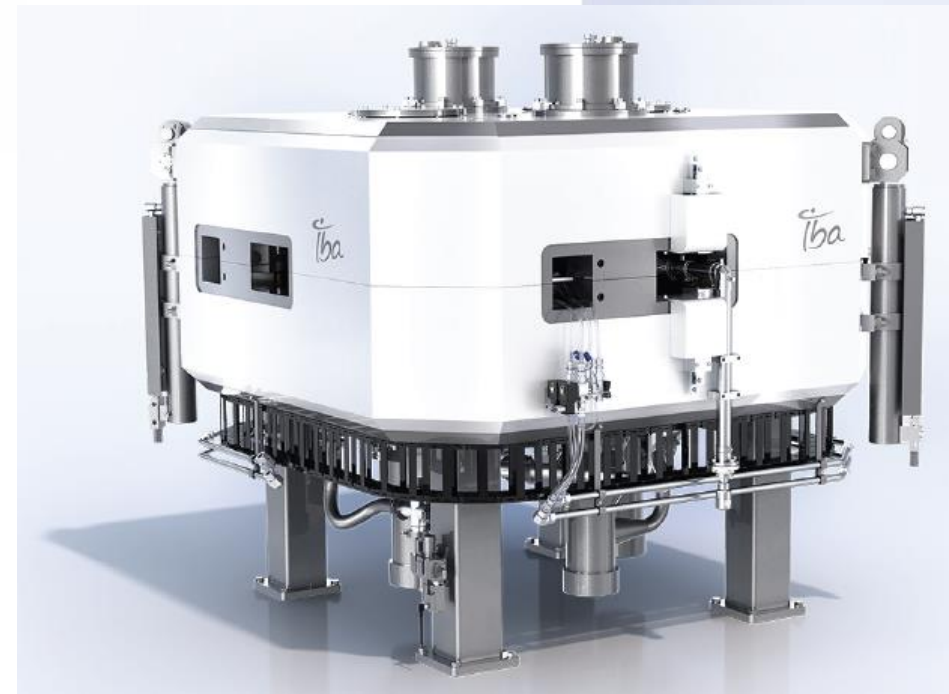
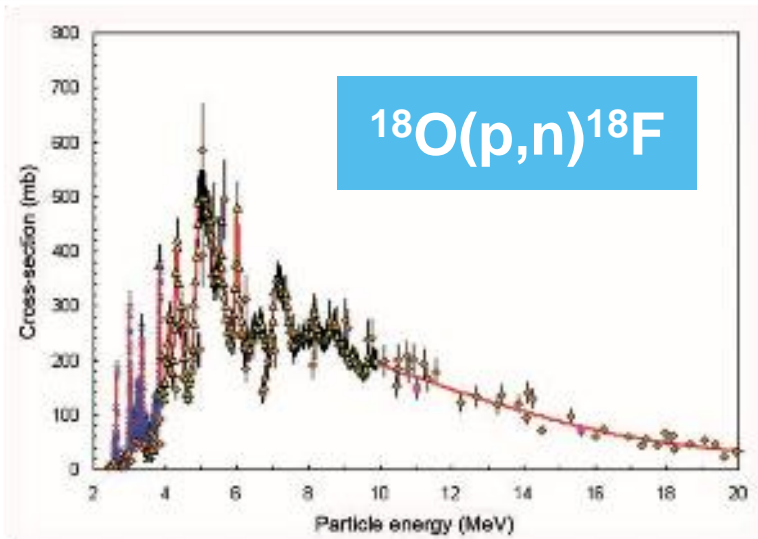
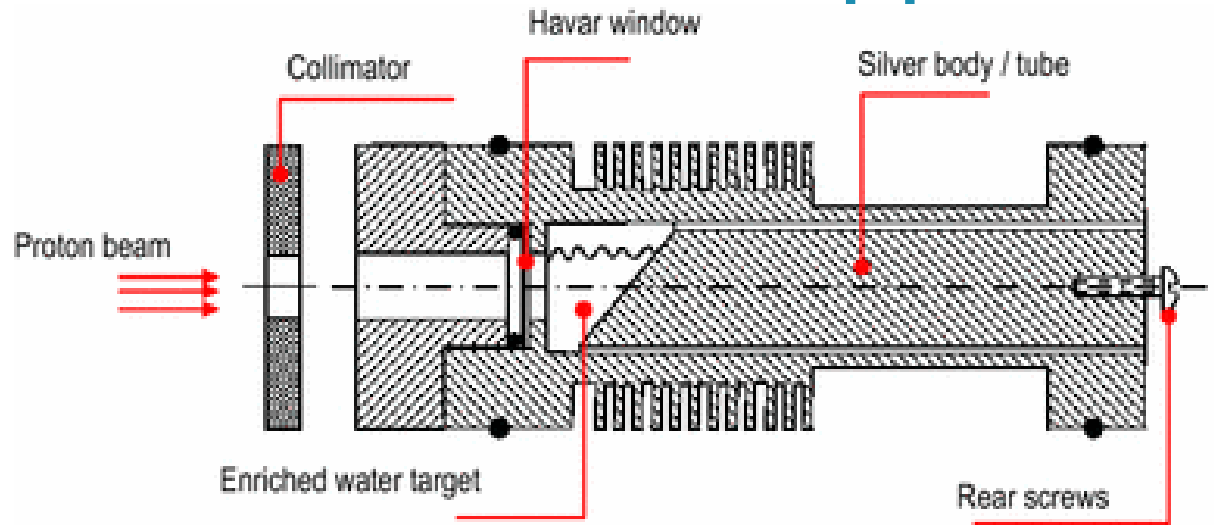
# Industrial production

# Case study: $^{60}\text{Co}$

- $^{59}\text{Co} (n,\gamma) ^{60}\text{Co}$  at nuclear reactors
- $T_{1/2} = 5.27 \text{ y}$  vs full transmutation in a few months
  - ▶  $\lambda = 4.2 \times 10^{-9} \text{ Hz}$
  - ▶  $\varphi\sigma \sim 3 \times 10^{-7} \text{ Hz}$  dominates
    - Specific activity is highest achievable on the account that the whole mass is radioactive. Samples can reach up to 900 Ci/g.
- Other reactions can happen such as  $^{60}\text{Co} (n,\gamma) ^{61}\text{Co}$ 
  - ▶  $T_{1/2} = 1.6\text{h} \rightarrow$  small waiting time can yield 100% purity
  - ▶ The specific activity is reduced accordingly

$$1 \text{ Ci} = 3.7 \cdot 10^{10} \text{ Bq} = 37 \text{ GBq}$$

# $^{18}\text{F}$ for medical applications



# Towards $^{100}\text{Sn}$

- How it was produced so far
- Up and coming: S3 at GANIL

# $^{100}\text{Sn}$ as seen in GSI

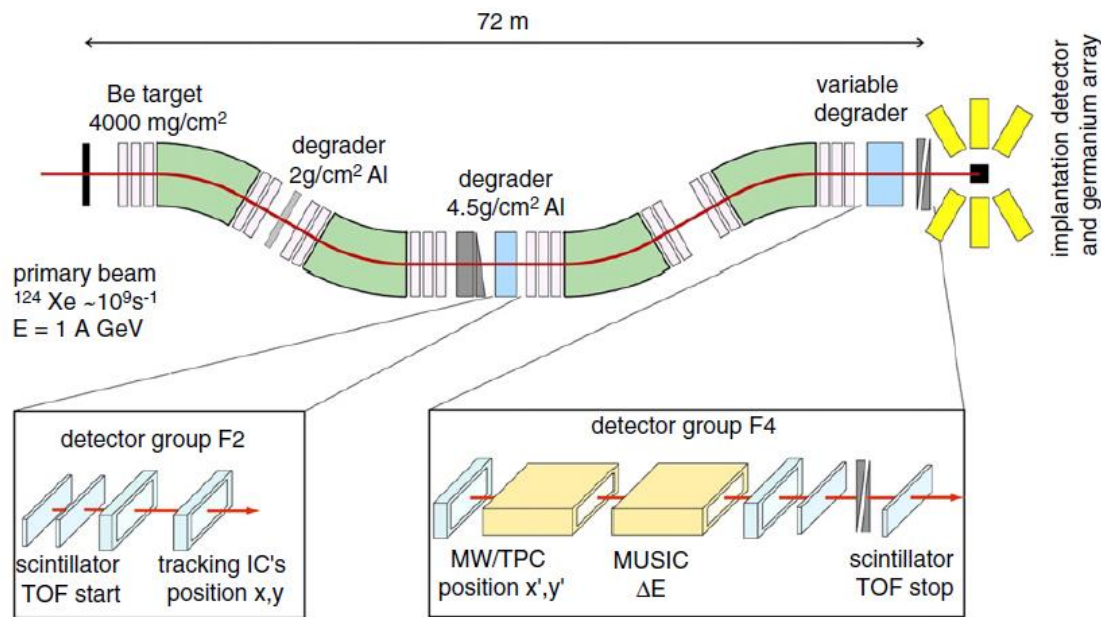


Fig. 2.4.1. The fragment separator FRS at GSI [97].

$^{124}\text{Xe}$  fragmentation  
0.16 pnA

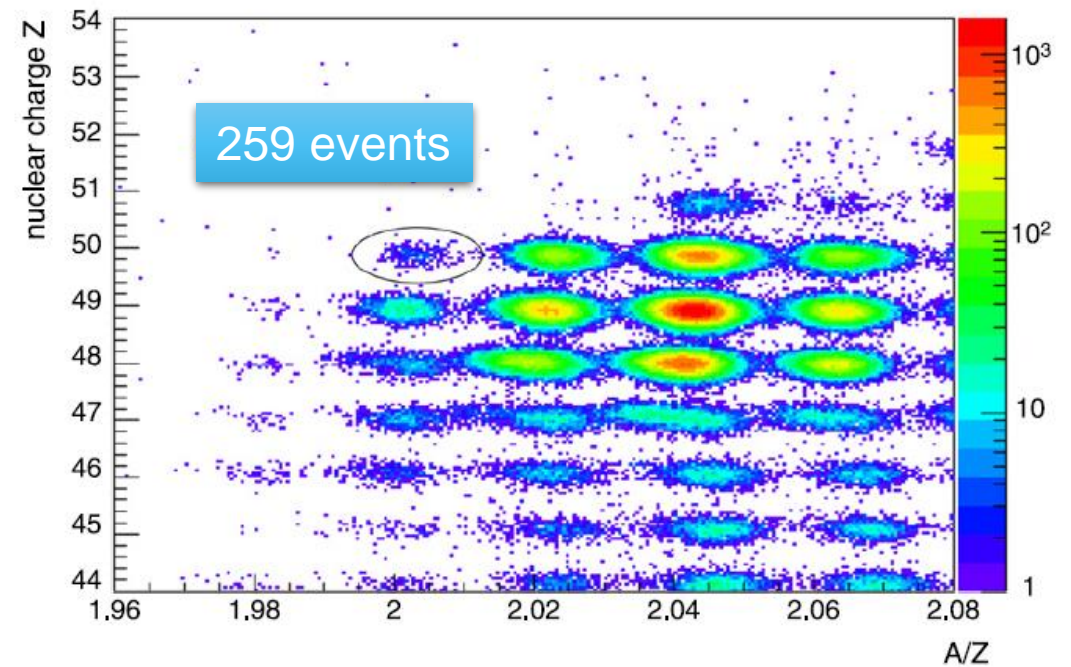


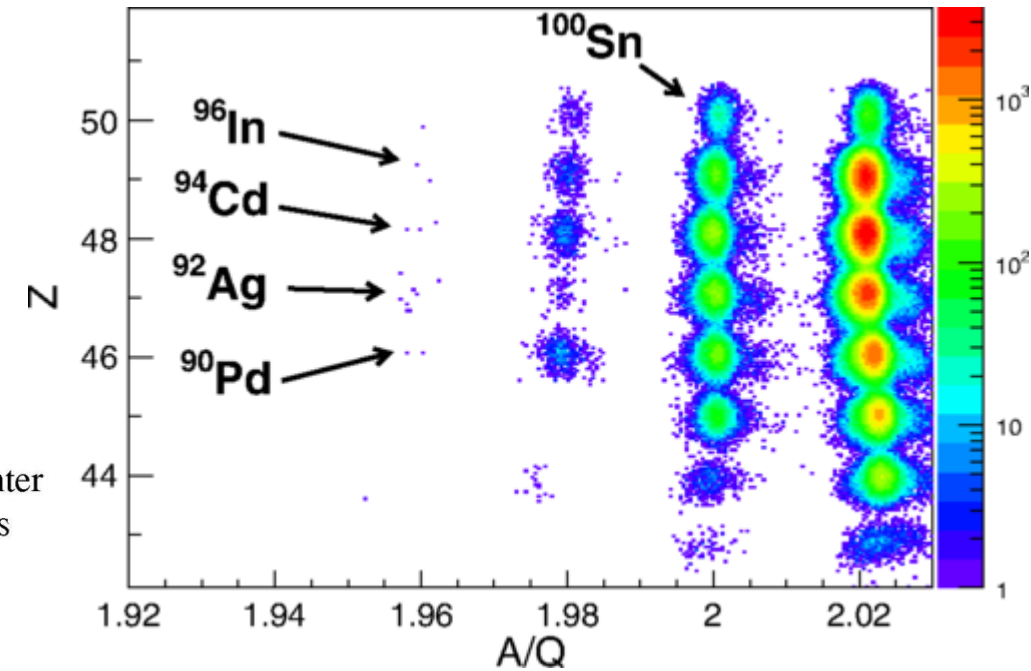
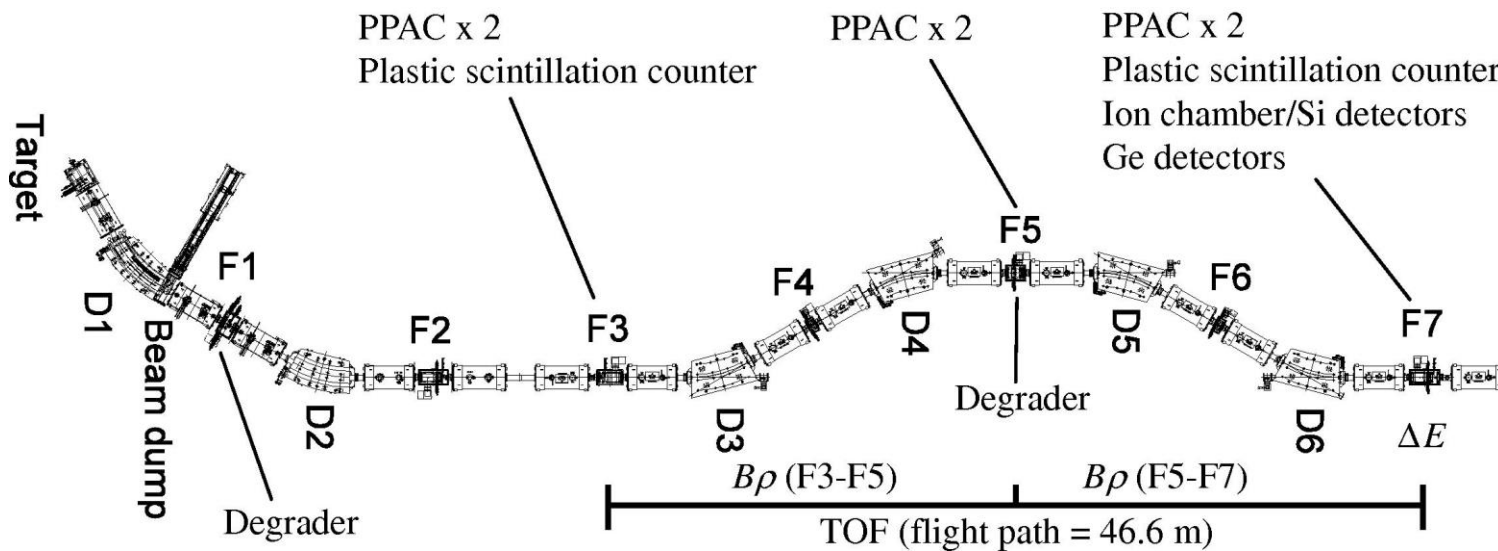
Fig. 2.4.2. Identification plot of  $^{124}\text{Xe}$  fragmentation at GSI [33].  $^{100}\text{Sn}$  events are encircled.



# $^{100}\text{Sn}$ with EURICA & WAS3ABi at RIKEN

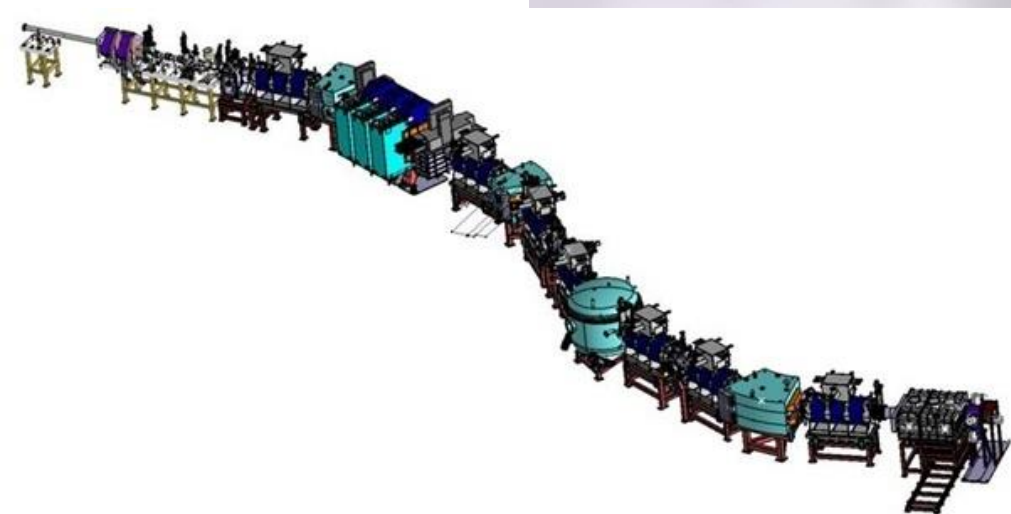
2500 events

$^{124}\text{Xe}$  fragmentation  
36 pA





# $^{100}\text{Sn}$ tomorrow: $S^3$ at GANIL



$^{58}\text{Ni}(^{50}\text{Cr},x)^{100}\text{Sn}$  fusion-evaporation  
4.5 MeV/u  
4000 pnA

1-20 ions/s at the focal plane

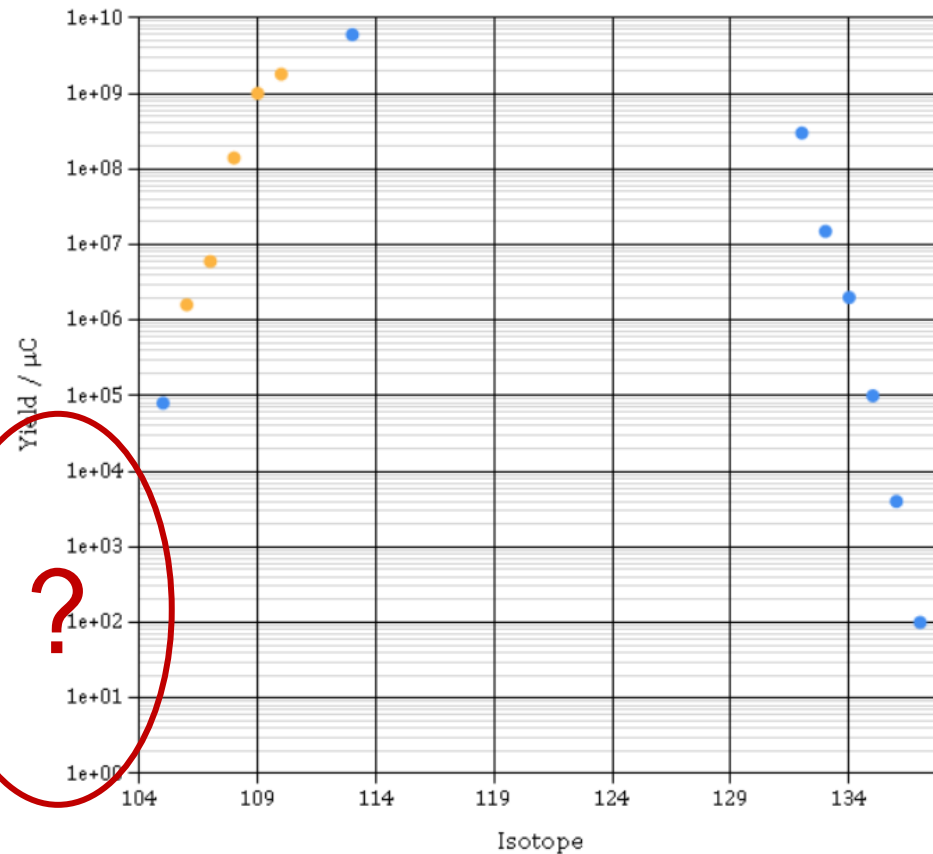


Could match the existing  
statistics in just over 2 minutes!

# $^{100}\text{Sn}$ at ISOL facilities?

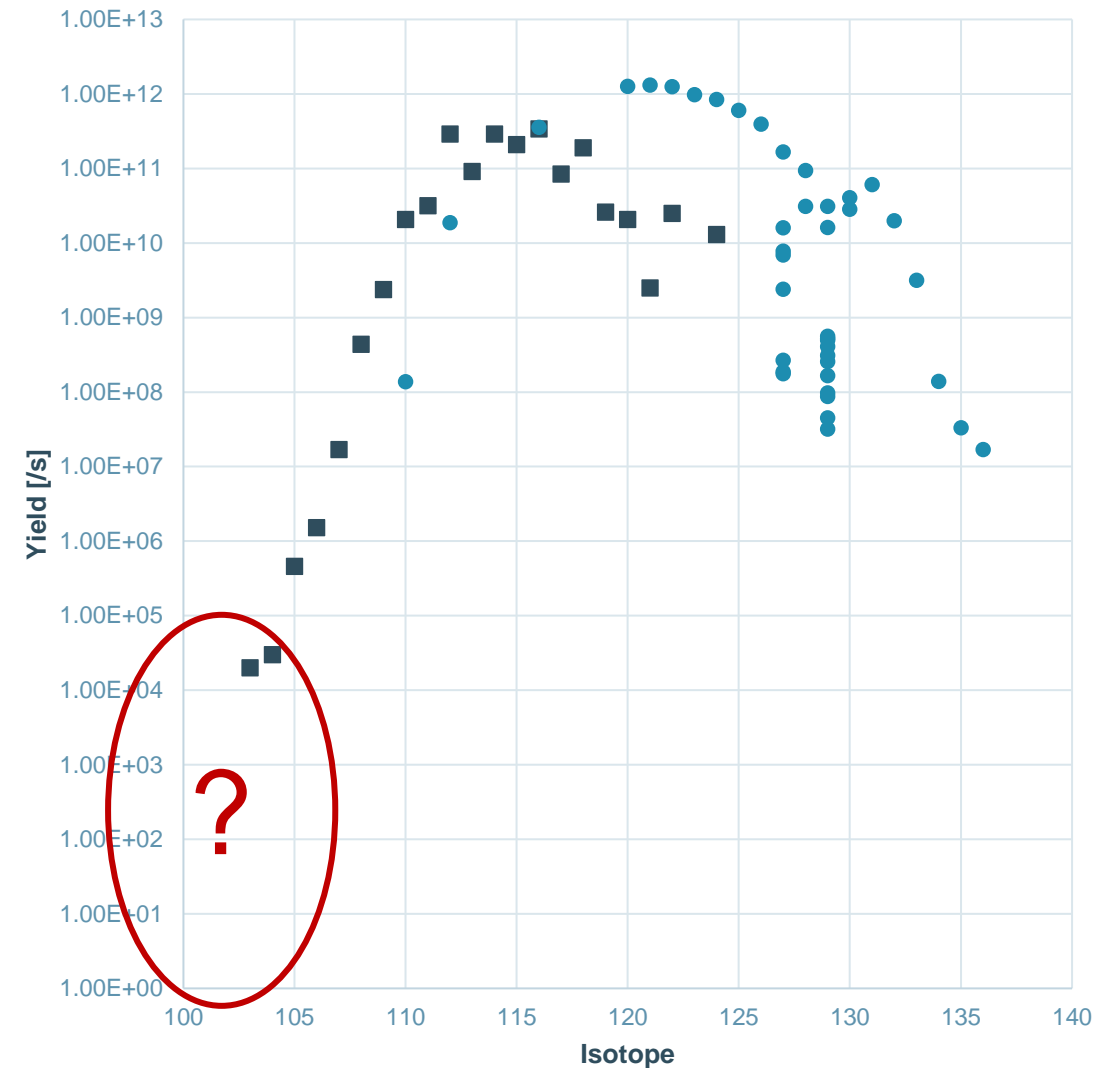
**ISOLDE**

● U Carbide (PSB) ● La Carbide (PSB)



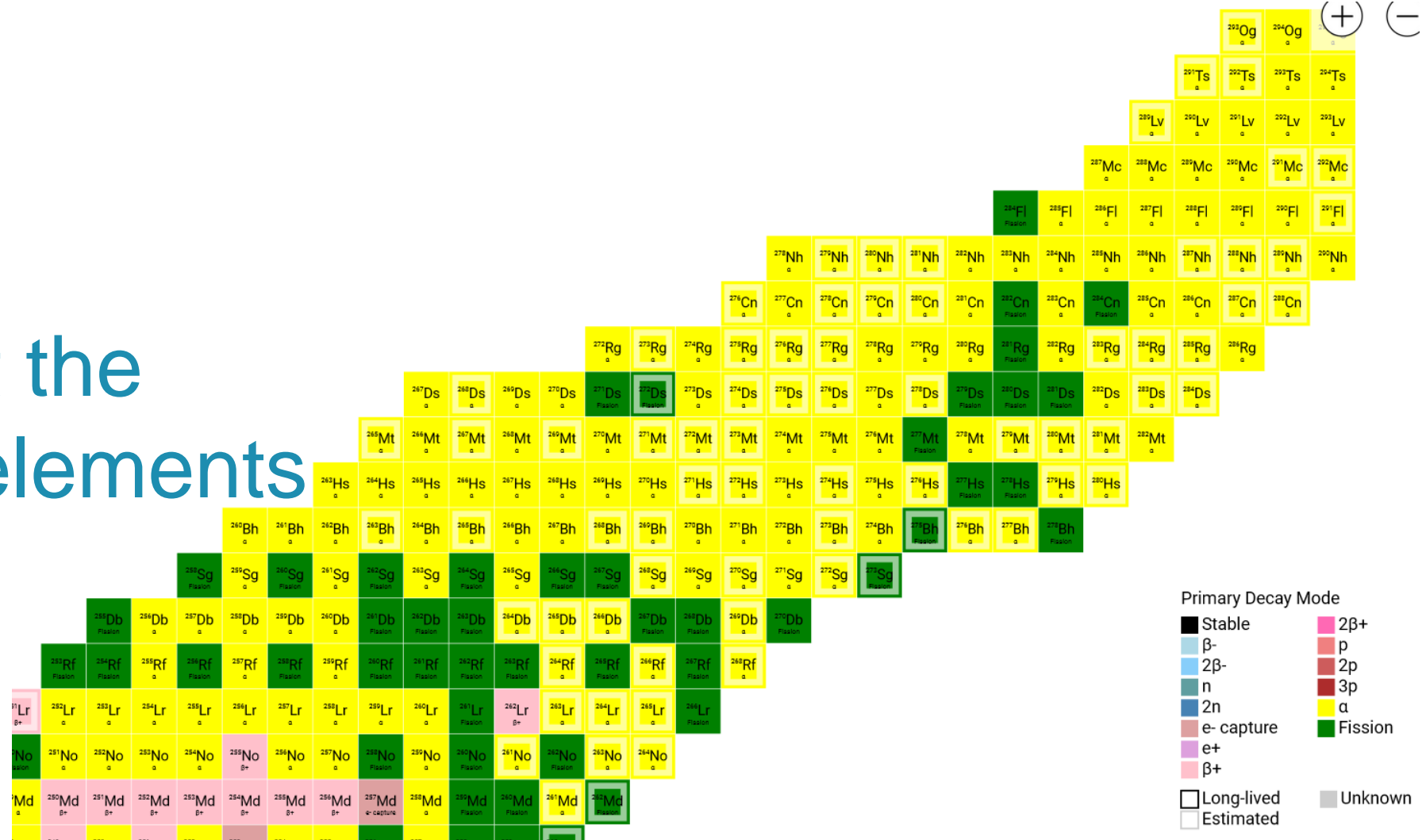
**TRIUMF**

■ Ta target ● U target



# Reaching out the superheavy elements

- Cold fusion
- Hot fusion

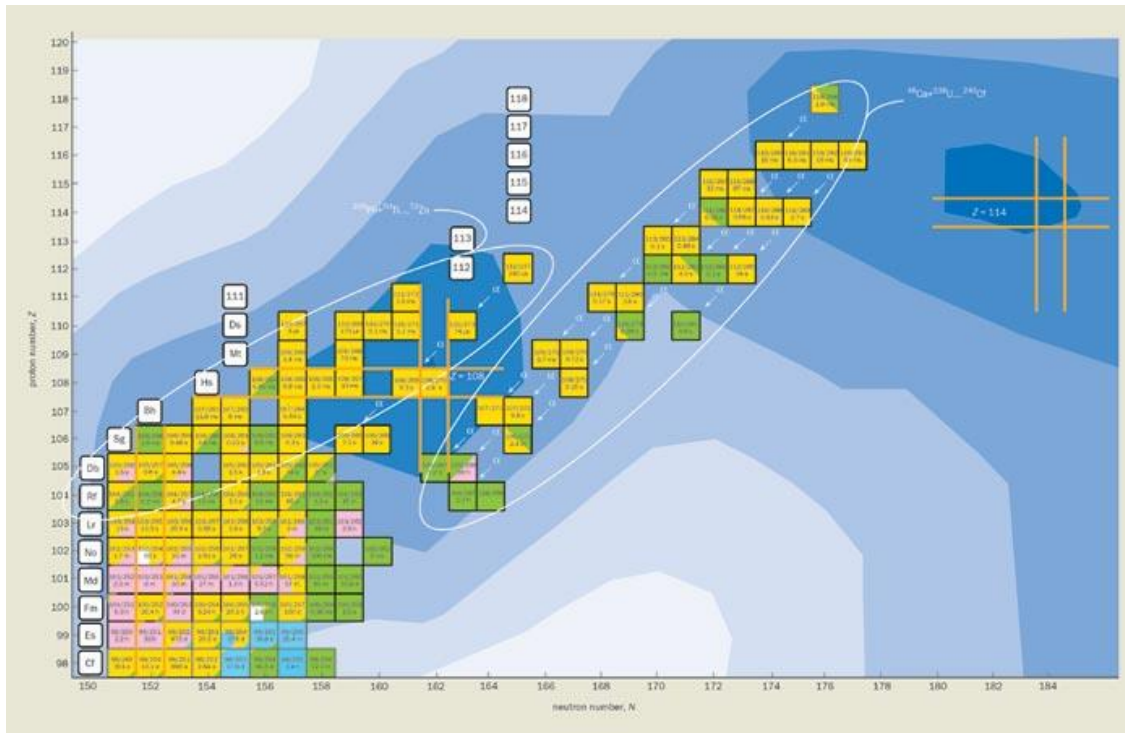


# The Periodic Table of Elements

scientificgems.wordpress.com

The Periodic Table of Elements																		scientificgems.wordpress.com																			
1 H Hydrogen																		2 He Helium																			
3 Li Lithium		4 Be Beryllium																		5 B Boron		6 C Carbon		7 N Nitrogen		8 O Oxygen		9 F Fluorine		10 Ne Neon							
11 Na Sodium		12 Mg Magnesium																		13 Al Aluminium		14 Si Silicon		15 P Phosphorus		16 S Sulfur		17 Cl Chlorine		18 Ar Argon							
19 K Potassium		20 Ca Calcium		21 Sc Scandium		22 Ti Titanium		23 V Vanadium		24 Cr Chromium		25 Mn Manganese		26 Fe Iron		27 Co Cobalt		28 Ni Nickel		29 Cu Copper		30 Zn Zinc		31 Ga Gallium		32 Ge Germanium		33 As Arsenic		34 Se Selenium		35 Br Bromine		36 Kr Krypton			
37 Rb Rubidium		38 Sr Strontium		39 Y Yttrium		40 Zr Zirconium		41 Nb Niobium		42 Mo Molybdenum		43 Tc Technetium		44 Ru Ruthenium		45 Rh Rhodium		46 Pd Palladium		47 Ag Silver		48 Cd Cadmium		49 In Indium		50 Sn Tin		51 Sb Antimony		52 Te Tellurium		53 I Iodine		54 Xe Xenon			
55 Cs Cesium		56 Ba Barium		57–71 La–Lu Lanthanides		Superheavy elements: $Z \geq 104$																79 Au Gold		80 Hg Mercury		81 Tl Thallium		82 Pb Lead		83 Bi Bismuth		84 Po Polonium		85 At Astatine		86 Rn Radon	
87 Fr Francium		88 Ra Radium		89–103 Ac–Lr Actinides		104 Rf Rutherfordium		105 Db Dubnium		106 Sg Seaborgium		107 Bh Bohrium		108 Hs Hassium		109 Mt Meitnerium		110 Ds Darmstadtium		111 Rg Roentgenium		112 Cn Copernicium		113 Nh Nihonium		114 Fl Flerovium		115 Mc Moscovium		116 Lv Livermorium		117 Ts Tennessine		118 Og Oganesson			
				57 La Lanthanum		58 Ce Cerium		59 Pr Praseodymium		60 Nd Neodymium		61 Pm Promethium		62 Sm Samarium		63 Eu Europium		64 Gd Gadolinium		65 Tb Terbium		66 Dy Dysprosium		67 Ho Holmium		68 Er Erbium		69 Tm Thulium		70 Yb Ytterbium		71 Lu Lutetium					
Actinides				89 Ac Actinium		90 Th Thorium		91 Pa Protactinium		92 U Uranium		93 Np Neptunium		94 Pu Plutonium		95 Am Americium		96 Cm Curium		97 Bk Berkelium		98 Cf Californium		99 Es Einsteinium		100 Fm Fermium		101 Md Mendelevium		102 No Nobelium		103 Lr Lawrencium					

# Producing superheavy elements



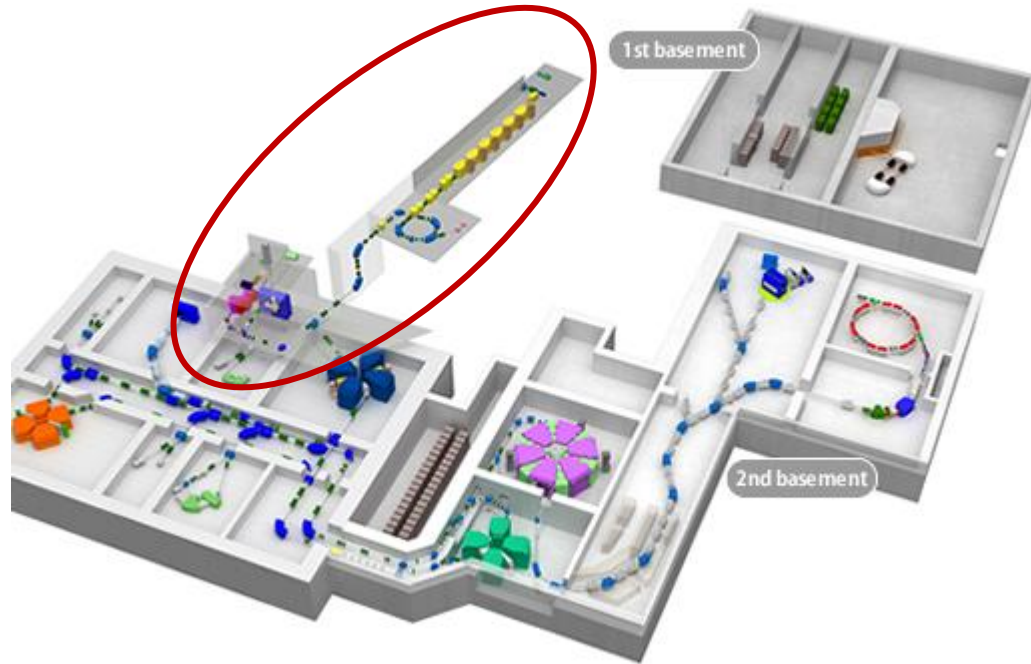
- Those can only be produced by ADDING matter together
  - Fusion(-evaporation) reactions
- Using stable beams on stable targets
  - Cold fusion, typically on  $^{208}\text{Pb}$  targets, with e.g.,  $^{70}\text{Zn}$  beams
- Using stable beams on actinide targets
  - Hot fusion, e.g., with  $^{48}\text{Ca}$  beams on a  $^{252}\text{Cf}$  target



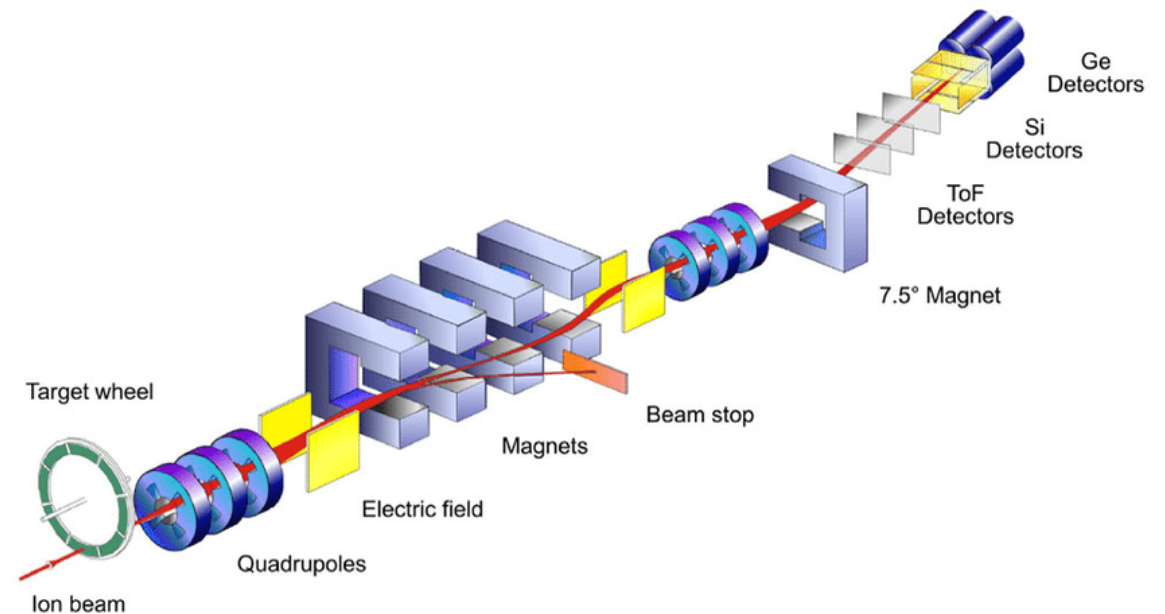
# Many facilities around the world

Combining  $^{48}\text{Ca}$  with actinide targets

## RIKEN GARIS & GARIS-II



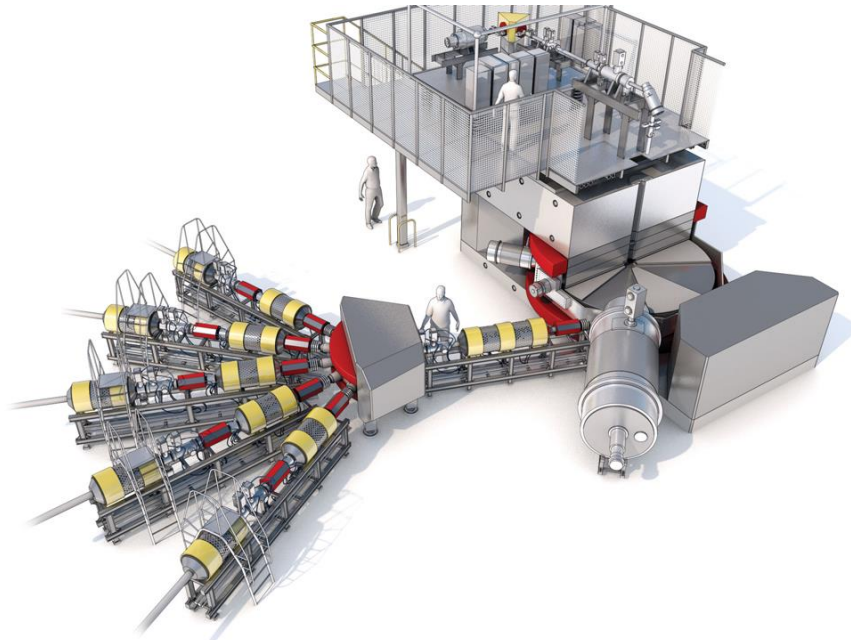
## GSI SHIP



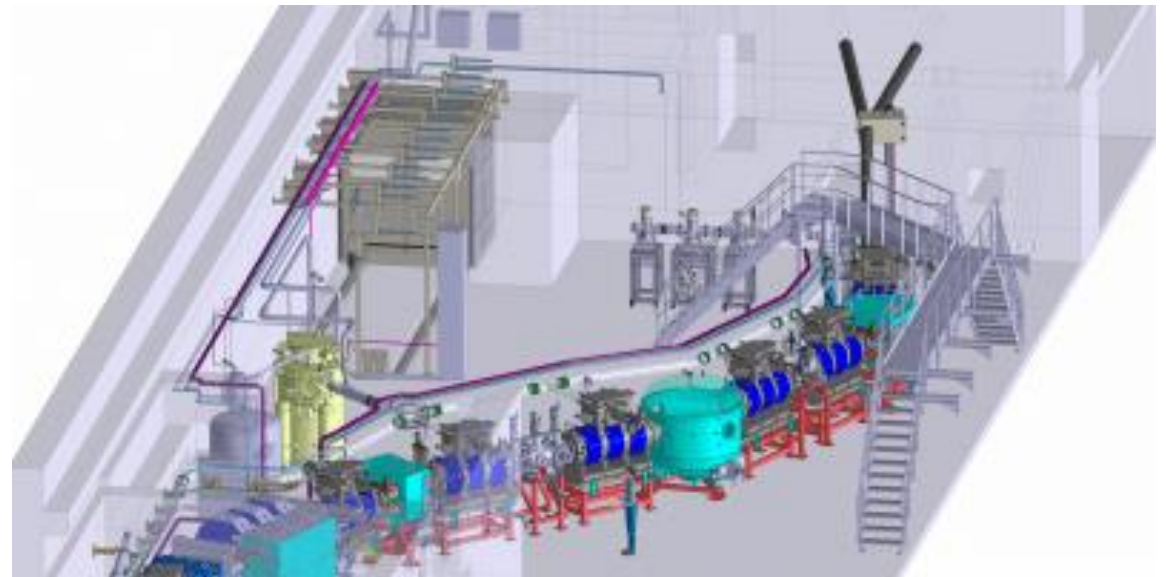
# Many facilities upcoming around the world

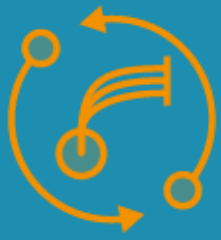
Combining  $^{48}\text{Ca}$  with actinide targets

## Dubna SHEF



## GANIL S<sup>3</sup>





- ✓ We have seen the different approaches to produce radioisotopes, first step towards radioactive beams.
  - ✓ We can either add particles (neutron capture, fusion-evaporation, *multi-nucleon transfer*) or break things apart (fragmentation, spallation, fission).
  - ✓ The production is a combination of the luminosity (beam and target content) and the reaction cross section. The half-life has also a substantial impact on what can be produced as well on the activity.
- 
- How that is used for the production of radioisotopes for applications
  - How  $^{100}\text{Sn}$  has been produced but also what to look forward to
  - The quest for superheavy elements

Recoil separators



# To be continued in the next lecture series

✓ 25 Oct 2021

## 1 – Basics of RIB production

- Nuclear reactions for the production of radioisotopes
- Luminosity & cross sections
- Examples across the nuclear landscape
  - Industrial production
  - Towards  $^{100}\text{Sn}$
  - Superheavy elements

▶ 8 Nov 2021

## 2 – State of the art in ISOL

- Target materials
  - Basic concepts
  - Innovative concepts
- Ion sources
  - Ultra pure beams
  - High intensity beams
- Beam manipulation
- Beam post-acceleration